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**ANALYSIS OF CONCRETE STRUCTURES  
BY FRACTURE MECHANICS**

**Proceedings from a RILEM Workshop dedicated to  
Professor Arne Hillerborg**

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**Edited by**

**Lennart Elfgren and Surendra P. Shah**

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