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WHY FRACKING WORKS AND WHY NOT WELL ENOUGH

ZDENĚK P. BAŽANT

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SPONSORS: DoE, LANL AND NU-ISEN

UNIVERSITY OF CALIFORNIA SAN DIEGO, CE SEMINAR, FEB. 11, 2015

Motivation

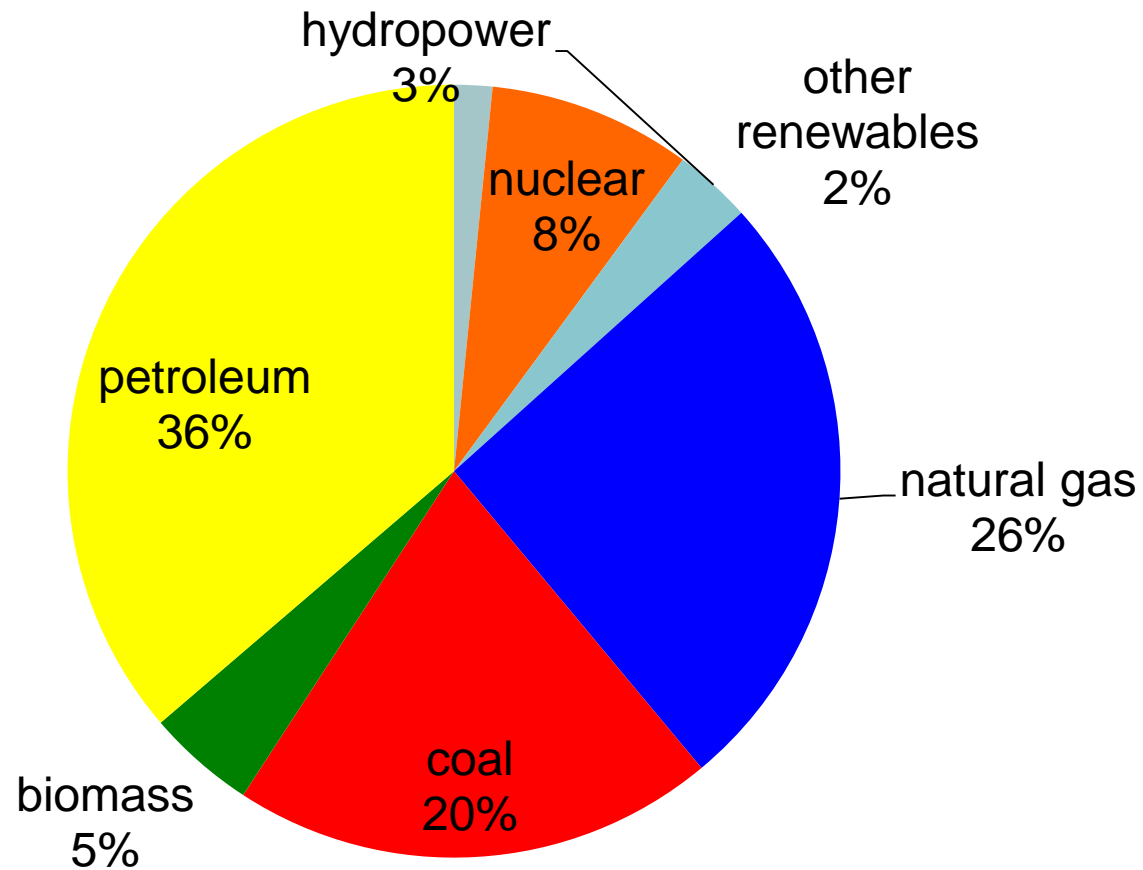
*The advances in hydraulic fracturing technology have been astonishing. **The impact on the national and world economies and geopolitical situation is amazing.***

*Although many aspects of the technology are well understood, the **fracture mechanics is not.***

Progress should increase the gas extraction percentage above current 5—15 %. This would also reduce the environmental footprint.

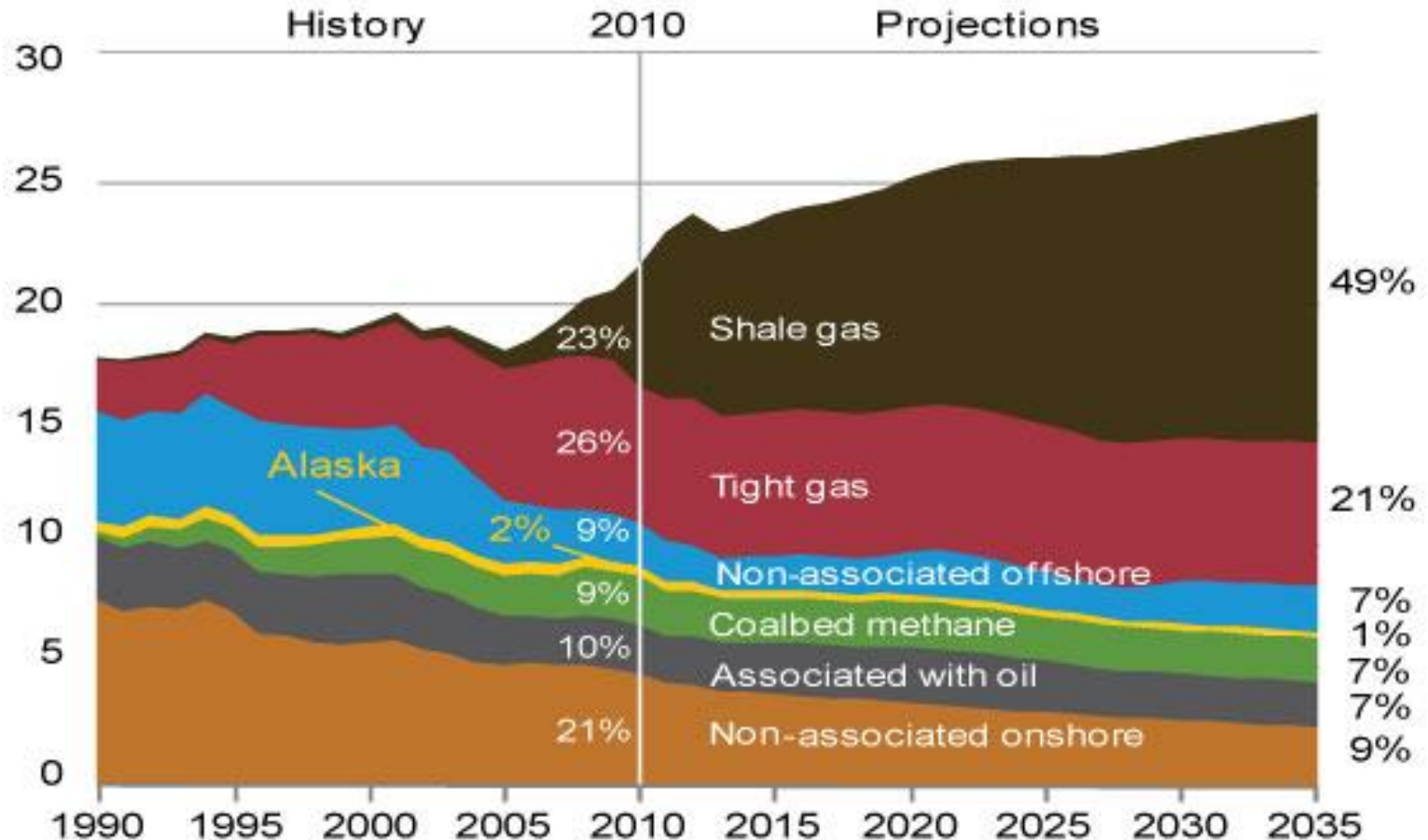
*Aperçu of
Hydraulic Fracturing
Technology
(aka “Fracking”)*

Where do we get our energy?



U.S. Natural Gas Production, 1990-2035

trillion cubic feet

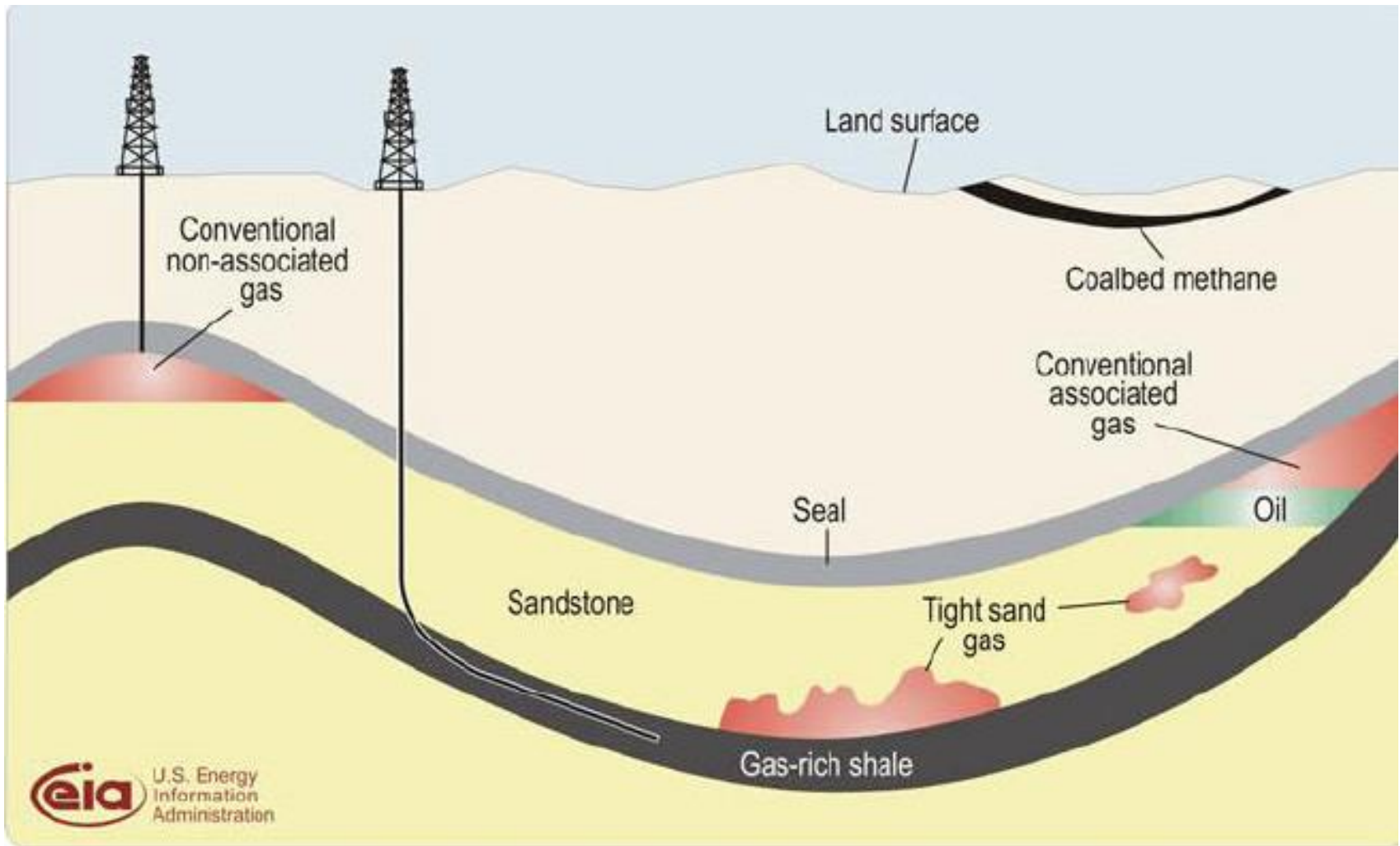


Source: U.S. Energy Information Administration, AEO2012 Early Release Overview, January 23, 2012.

Provenance of Natural Gas

- Formed by organic matter (marine organisms, plants) trapped in sedimentary rocks
- “Conventional” natural gas is trapped in porous rock—sandstone domes
- “Unconventional” natural gas is trapped in micropores of tighter rocks and in nanopores of shale

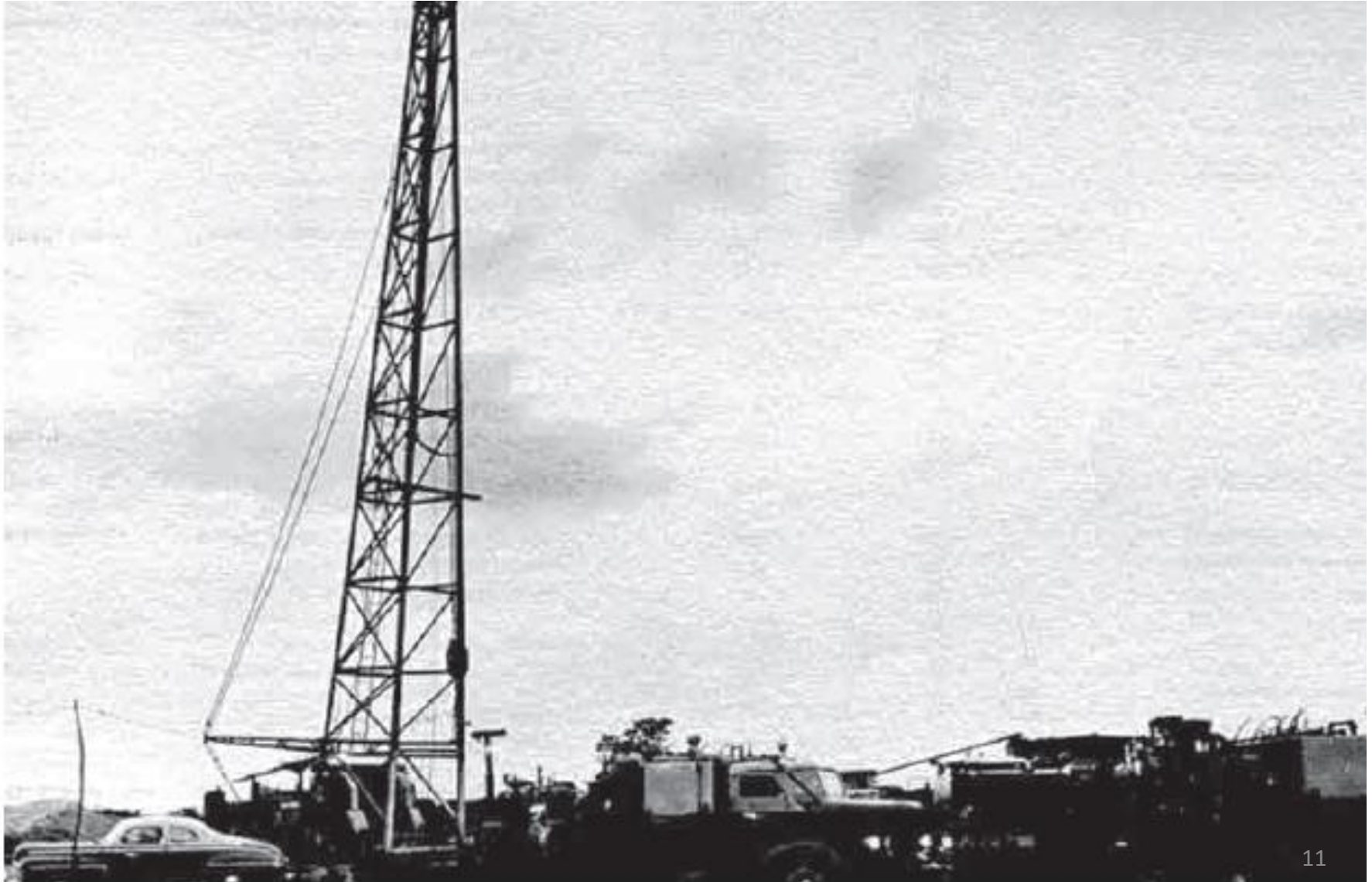
Schematic of Natural Gas Resources



History: 1947, Hugoton, Texas: Hydraulic Fracturing with Sand Proppant



1949: Halliburton conducts fracking in Archer County, Texas



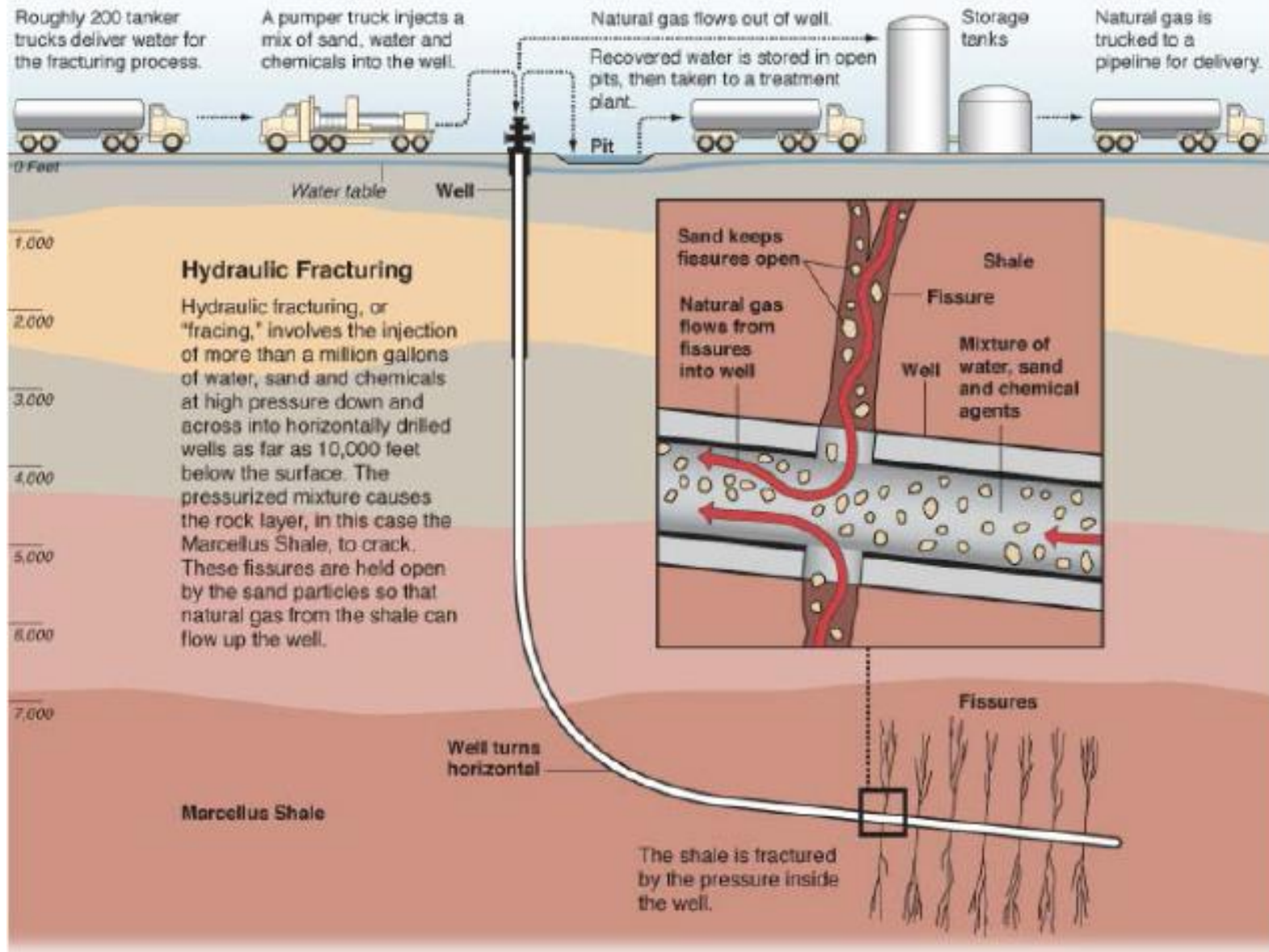
1955 Mass production of truck-mounted fracking pumps of 1475 HP, remotely controlled



Development and Features of Fracking

- Has been developed gradually **since 1947**, without government support (except recently, after success became obvious).
- Fracking involves:
 - Drilling a well, to reach shale layer typically 3 km down
 - **Turning drill to horizontal**, extending it for a few km
 - Injecting fluid under pressures up to about 25 MPa at pump—cca 2 mil. gal., which ***equals 1.7 mm of rain*** over lease area, per stage. The fluid is 99% water, plus chemicals and proppant (fine sand, < 1mm dia.). Only about 15% returns to the surface.
 - Extracting the gas, reinjecting contaminated water

Overall Scheme of Gas Extraction



Horizontal hydraulic hydrofracturing. Courtesy www.propublica.org/special/hydraulic-fracturing

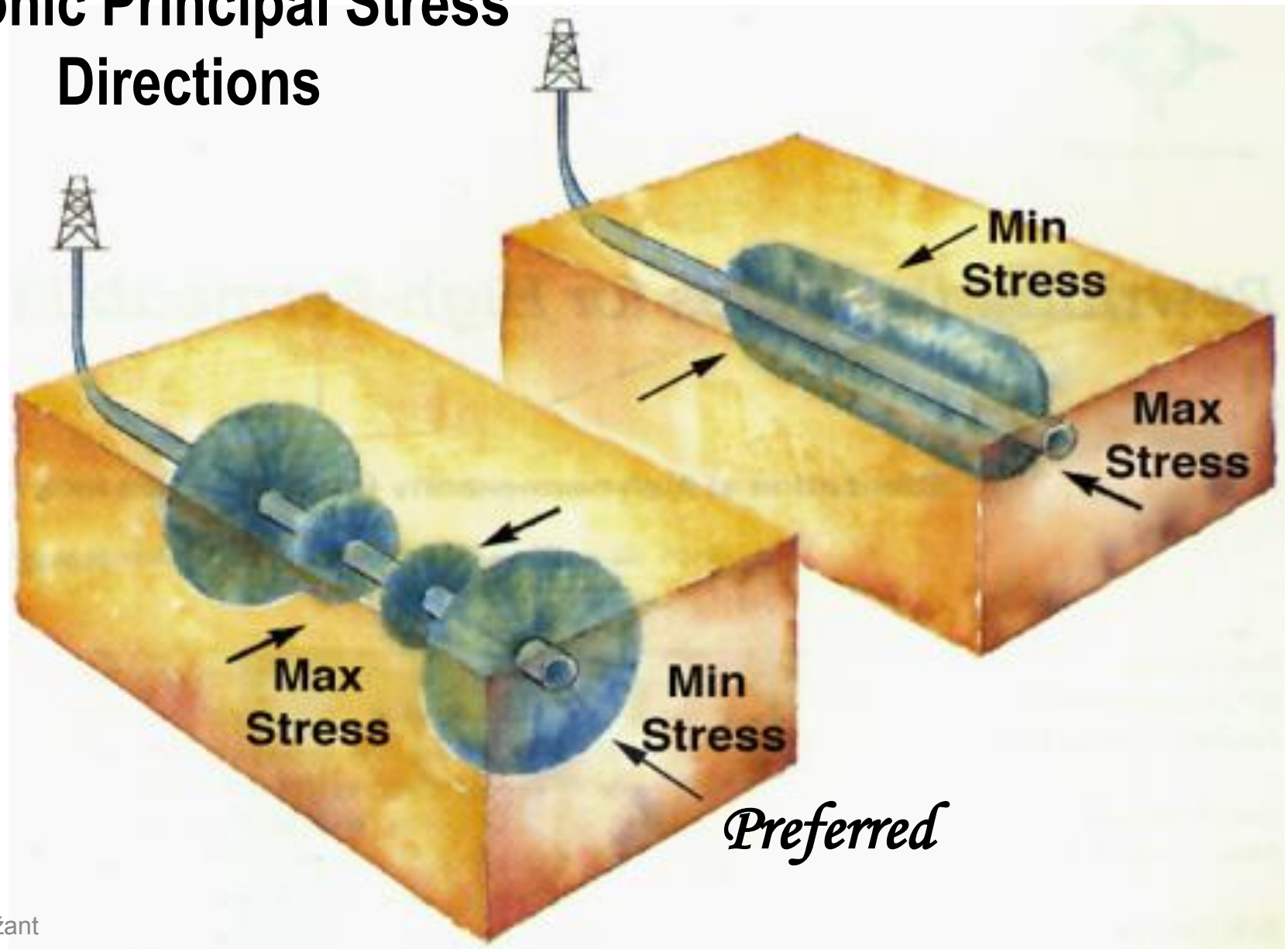
Horizontal Drilling

(Marcellus Shale)

- vastly enlarges gas extraction zone
- vastly reduces devastation on earth surface
- The well bore is turned to **horizontal** with a **radius big enough** for the high-strength steel pipe to remain elastic (typical pipe dia. 3.5 in.).

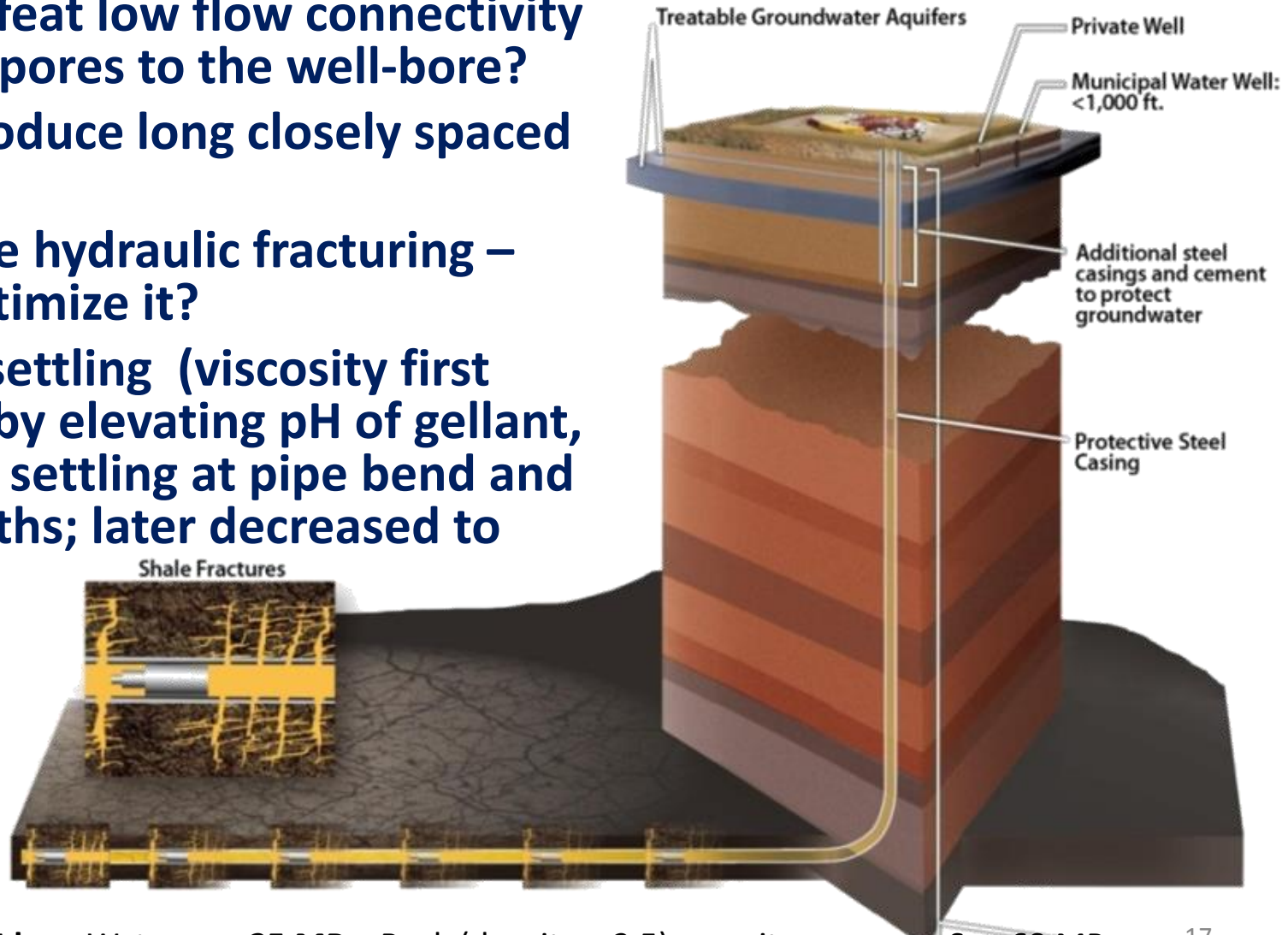


Horizontal Well-Bore vs. Tectonic Principal Stress Directions



Drilling and Fracking Operations

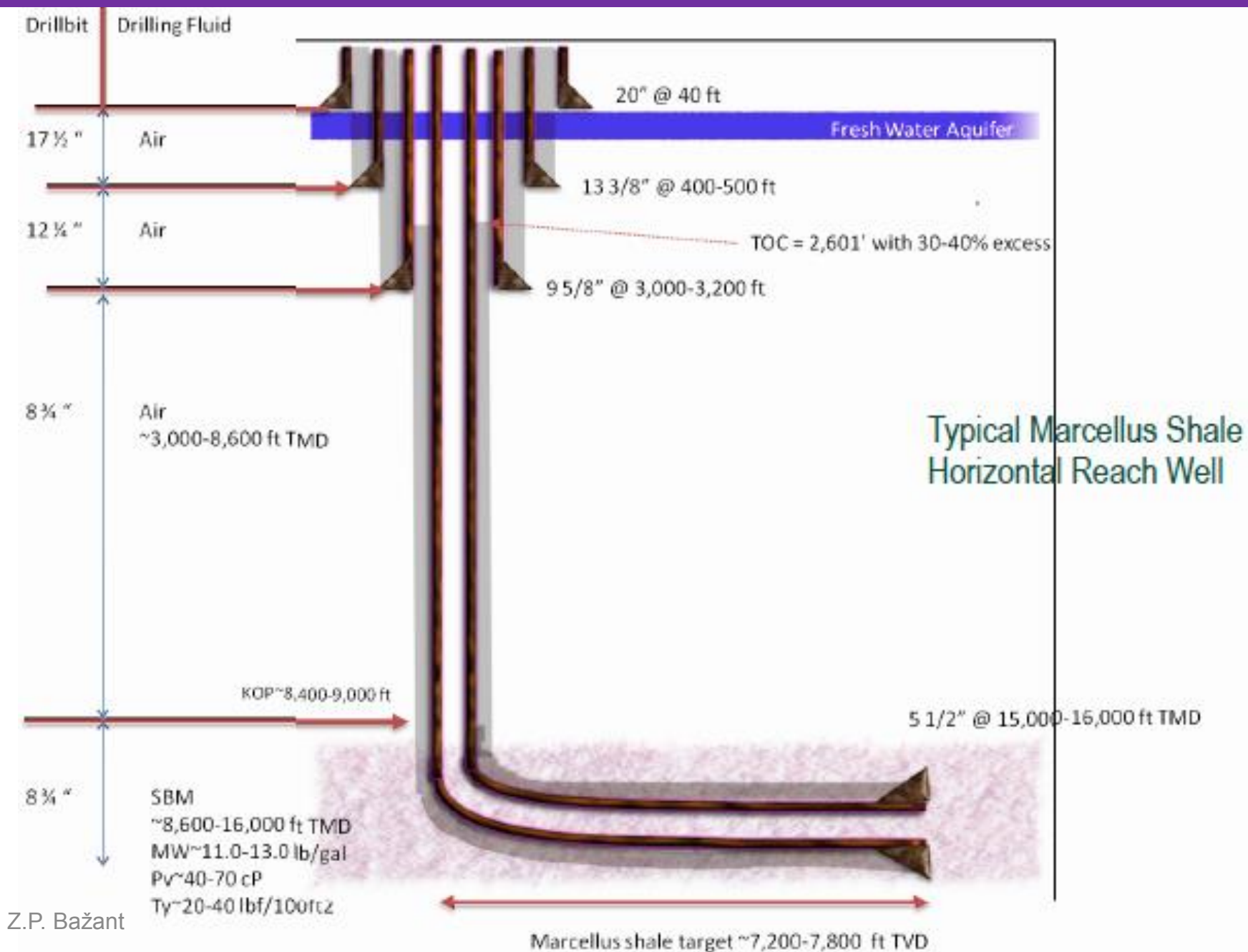
- How to defeat low flow connectivity from nanopores to the well-bore?
- How to produce long closely spaced cracks?
- Multi-stage hydraulic fracturing – how to optimize it?
- Proppant settling (viscosity first increased by elevating pH of gellant, to prevent settling at pipe bend and crack mouths; later decreased to penetrate deeper).
- etc.



Z.P. Bažant

At depth **2.5 km**: Water $p = 25 \text{ MPa}$, Rock (density ~ 2.5): gravity pressure $S_z \approx 68 \text{ MPa}$, Tectonic pressures = 55 and 42 MPa, Pump: 25 MPa, Pump + water pressure = 25+25 MPa (more with drilling mud). Shale density = 2 to 2.7, typical 2.5. (cf. granite 2.75)

TYPICAL SHALE-GAS WELL DIAGRAM



Undesirable Side Effects of Proppant

Congregation of proppant in the opened crack creates a steep pressure gradient.

If that happens at the crack tip, an event called in industry the “screen out”, hydraulic fracturing “locks up” and pressure rises dramatically, leading to shut-down.

To avoid it, water without proppant is injected initially.

Typical Drill Pad and Extraction Site

Chem Truck

Data Van

Flowback Fluid
(to be re-injected for deep storage)

Sand Storage

Blender

Frac Fluid

Pumps

Wellhead



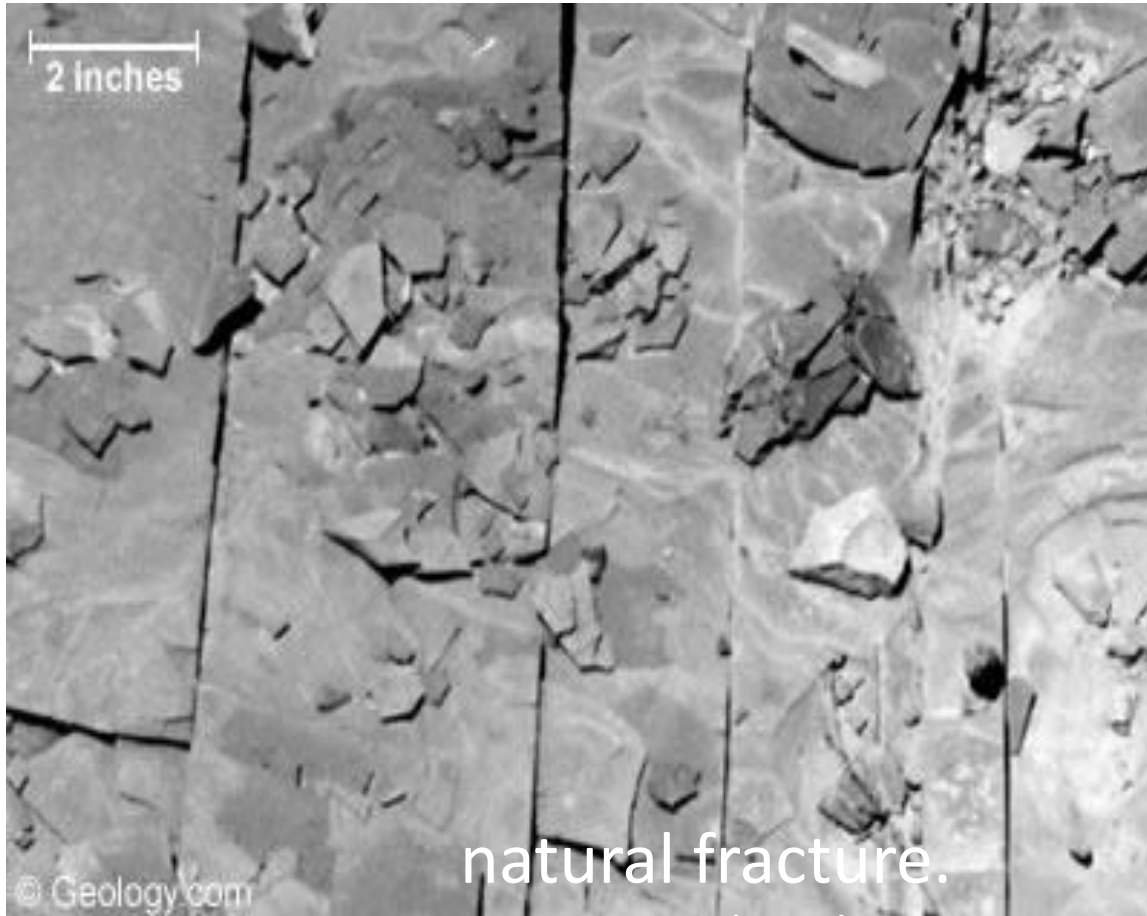
Fracking Fluid

Often a small amount of **polymer** is added as a **friction reducer**.

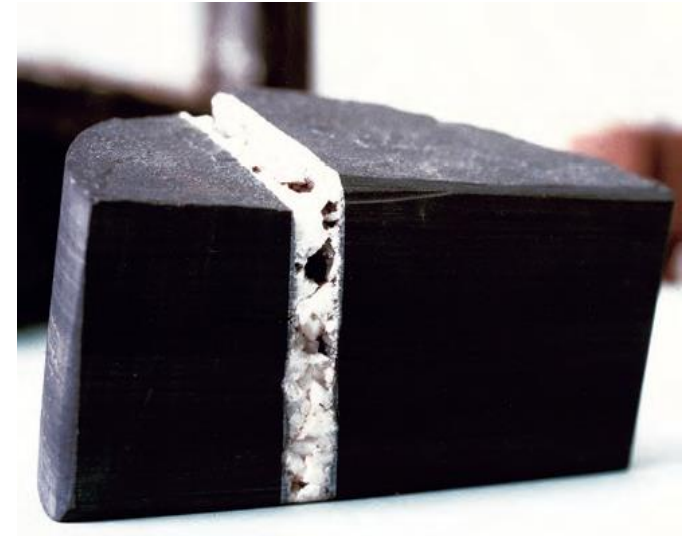
Usually a **gellant** (viscosifier) is added to limit proppant settling. It can be polymerized and its **viscosity** can be adjusted by **changing the pH** with borate or zirconium ions.



Vertical Joints in Devonian Shale (Marcellus)



Surface outcrop



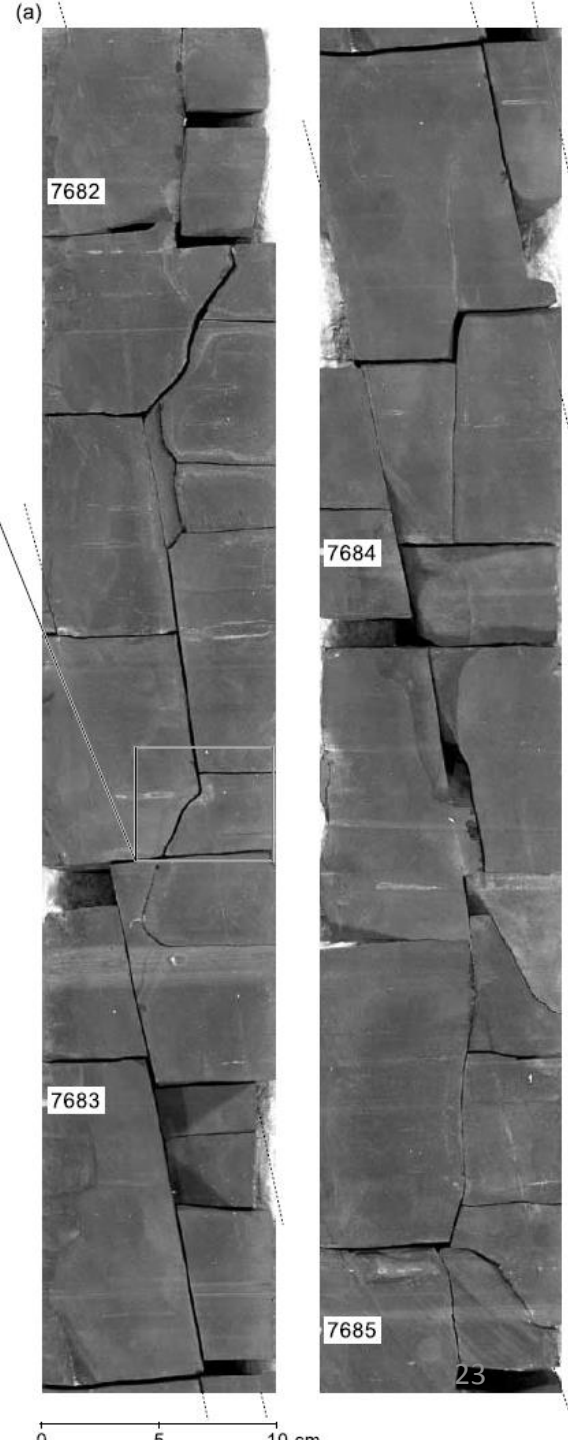
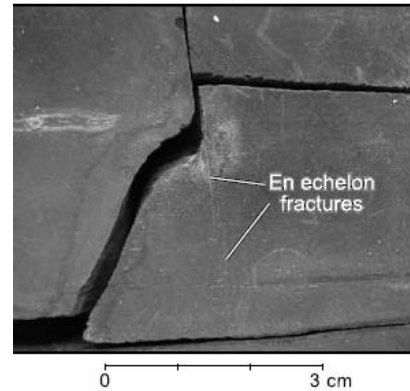
Drill core

(3.5 in. dia.) of Marcellus shale from West Virginia, with a joint filled by calcite

Natural Fractures in Shale Cores, Sealed with Calcite

Gale et al. (2007),
Am. Assoc. of
Petroleum Engrs.
Bulletin

From depth 2640 m



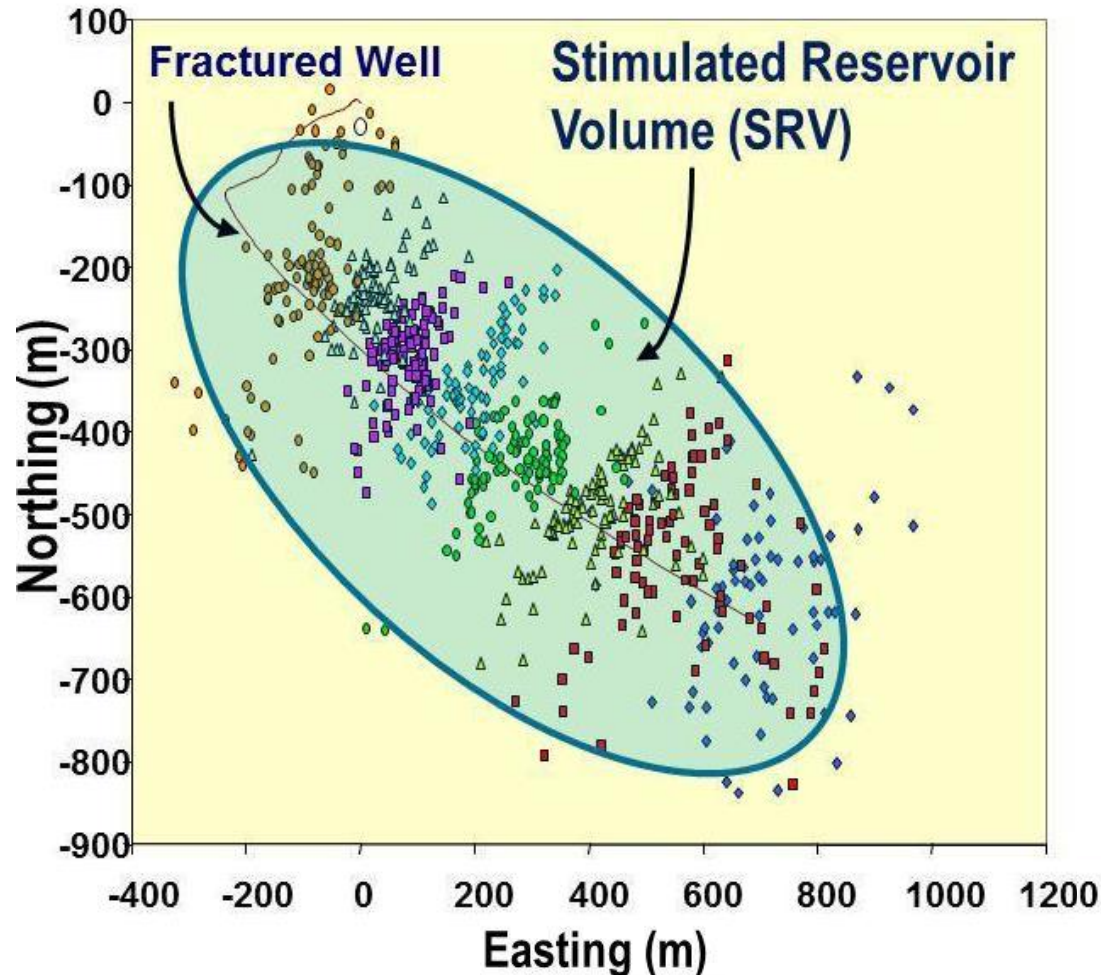
Weak horizontal bedding planes, subjected to large overburden pressure



- they cause **material orthotropy**, much more pronounced in strength and fracture properties than in elasticity

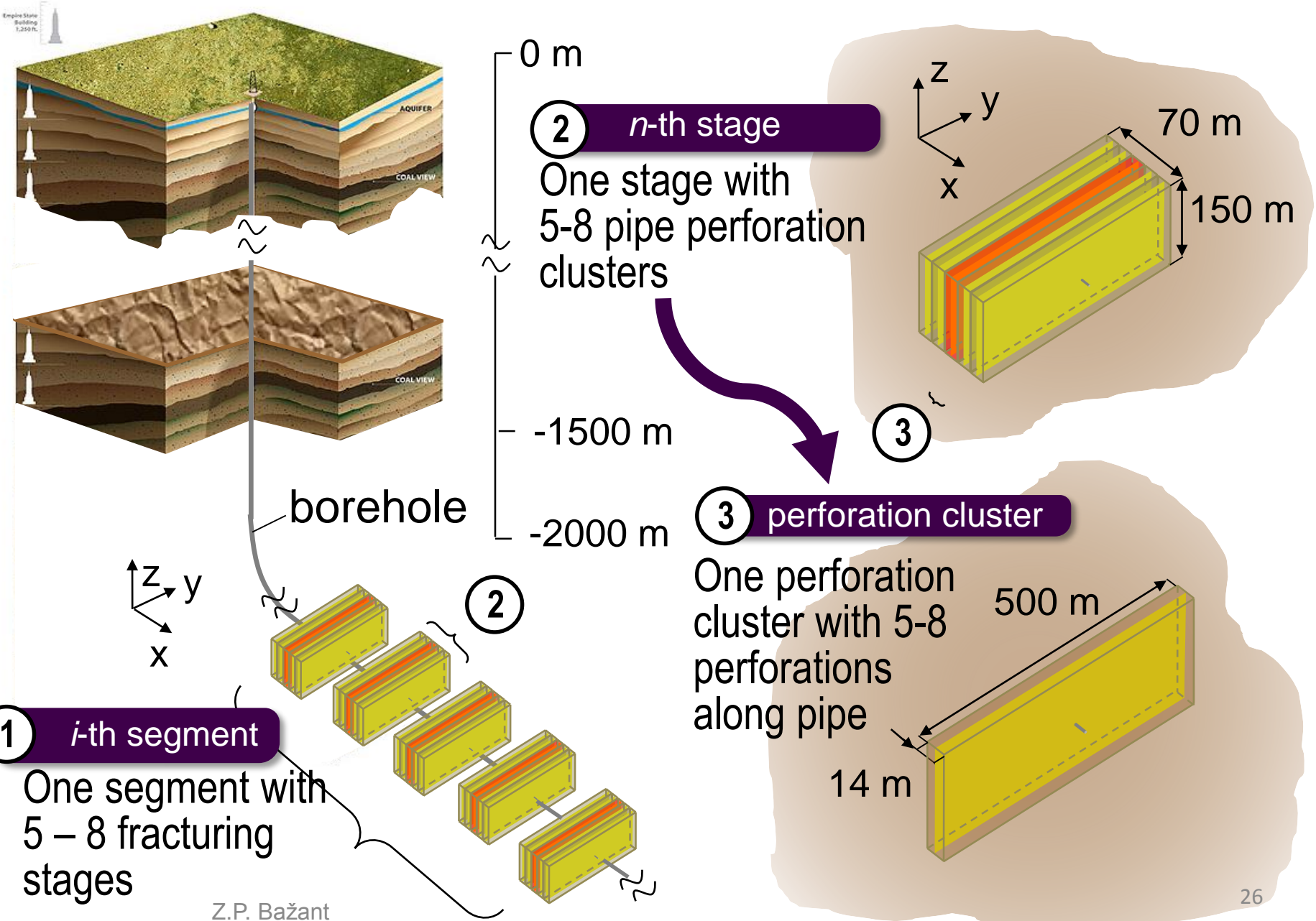
Microseismic sources in Marcellus shale reveal extent of fracturing

Plan view

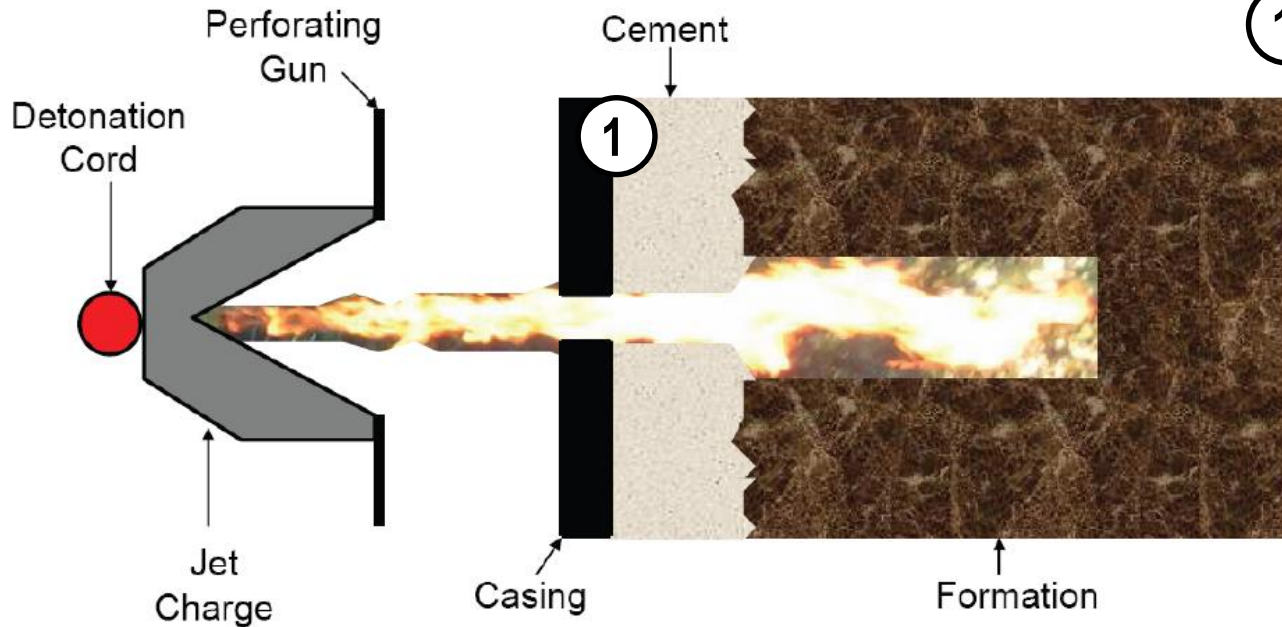


One segment with **12 stages** (each in a different color), each stage having **5 to 8 clusters**, each cluster having about **5 pipe perforations**

Main Features of the Well

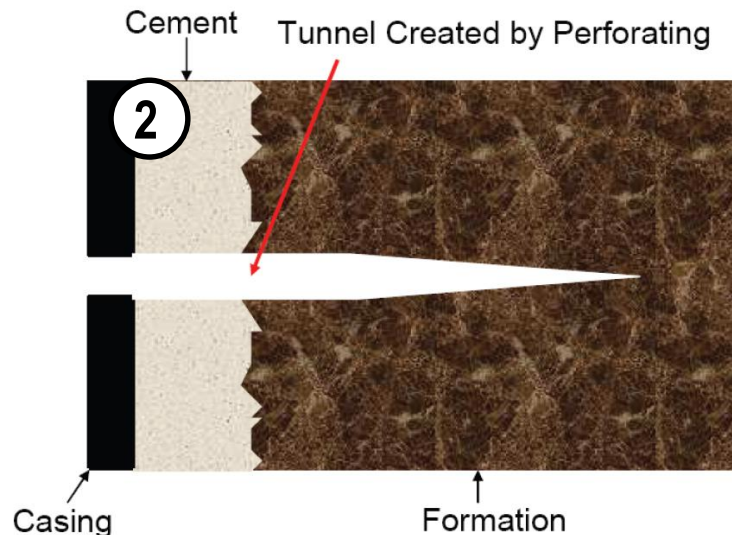


Perforation of High Strength Steel Pipe



① The shaped charge is detonated and a jet of very hot, high-pressure gas vaporizes the steel pipe, cement, and rock formation in its path

Common method:
jet-perforating guns
with explosive
shaped charges.



② Result: A tunnel, isolated by cement mortar, from production casing (or pipe) to rock formation.

Fracking works.

But why?

And why not well enough?

Usually, **only 5% to 15%** of gas gets extracted.
How to increase it?

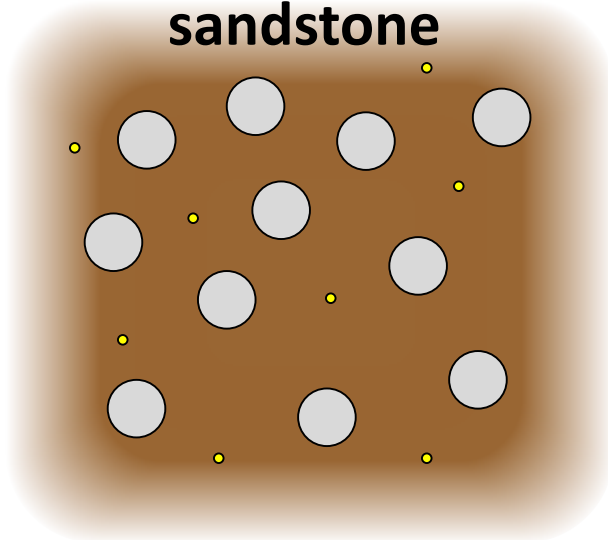
- 1) Increase the fracked volume fraction above 15%.
- 2) Achieve finer crack spacing.

*What is the spacing
of hydraulic cracks in shale?*

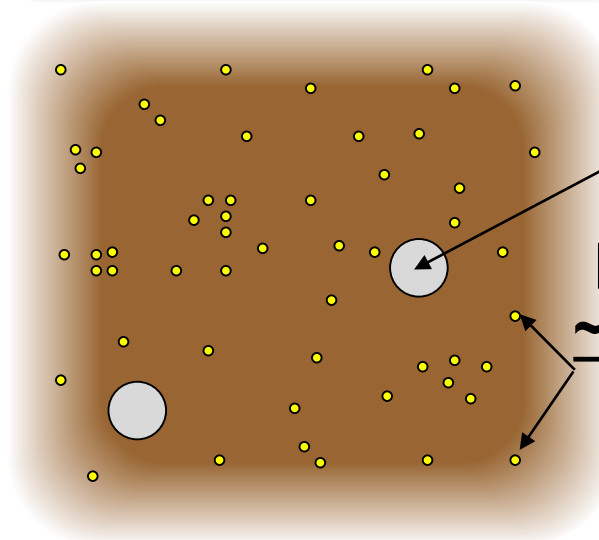
Shale permeability is extremely low

Conventional gas

sandstone



Shale gas



Micro-pores
(few, contain
little gas)

Nano-pores
~0.5 – 10 nm
diameter
(contain
most gas)

PERMEABILITY, b , in mD (miliDarcy)

Sandstones: $1 - 10^2$ (conventional gas)

Tight gas: $10^{-3} - 10^{-1}$

Concrete: $10^{-4} - 10^{-3}$

Shale: $10^{-6} - 10^{-5}$

The crack spacing can be deduced from:

1. Known percentage of gas extracted from the shale stratum — 15 %.
2. Time to reach maximum gas flux on the drillpad.
3. Halftime of flux rate decay on the drillpad.
4. Known permeability of shale.

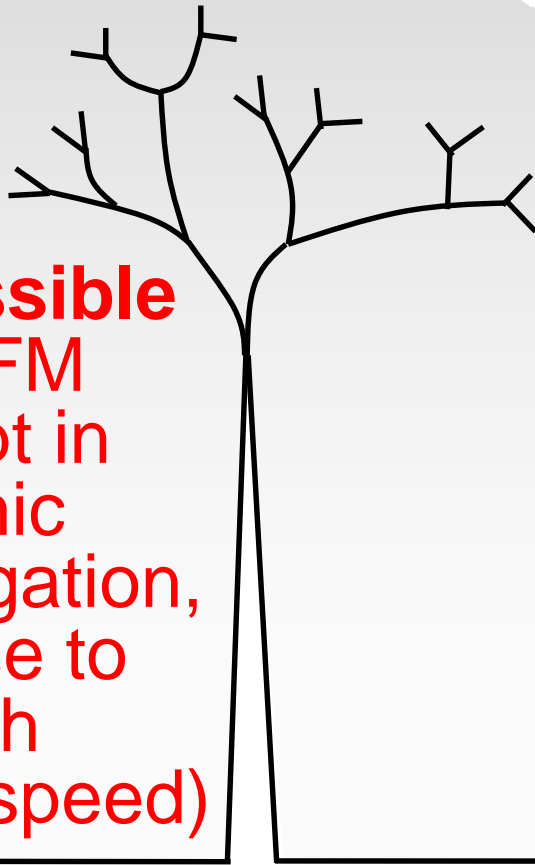
RESULT: Crack spacing = 10 cm (Fayetteville shale).

Crack Topology

(A)

Branching at crack tips?

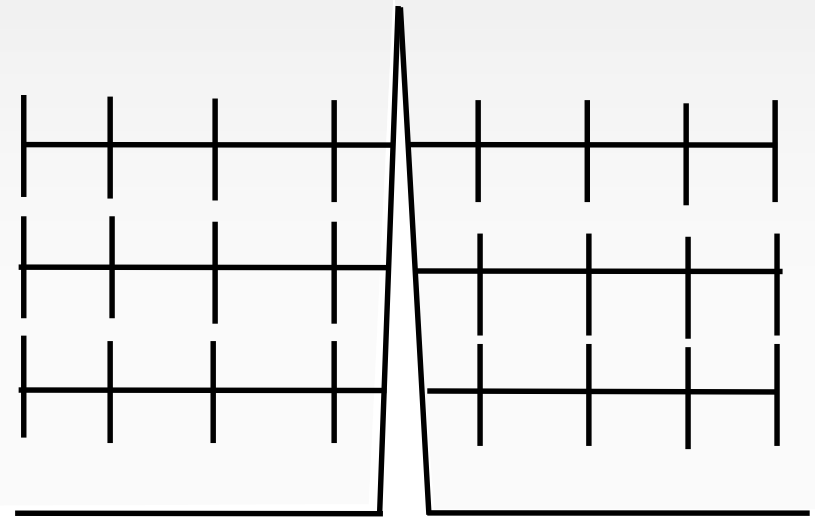
Impossible
by LEFM
(except in
dynamic
propagation,
at close to
Rayleigh
wave speed)



(B)

Nucleation from weak joints, faults, defects

Possible in statics
(fracking takes many days)



Gas Diffusion from Nanopores to Adjacent Cracks

Diffusion equation — nonlinear, **compressible** gas:

$$\frac{\phi}{k} \left(c_\phi + \frac{1}{p} \right) \mu \frac{\partial p}{\partial t} = \frac{\partial^2 p}{\partial x^2} + \frac{1}{p} \left(\frac{\partial p}{\partial x} \right)^2$$

Profiles of gas pressure p at subsequent times

Darcy gas flux:
$$q = -\frac{k}{\mu} \frac{\partial p}{\partial x}$$

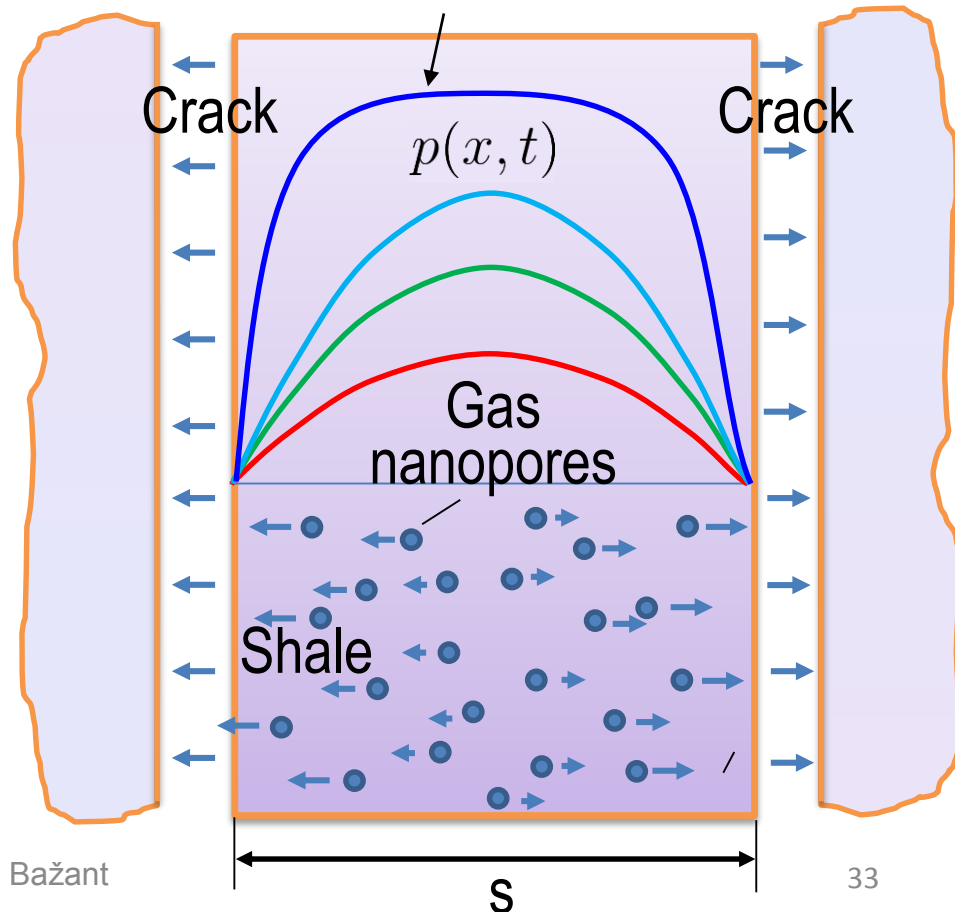
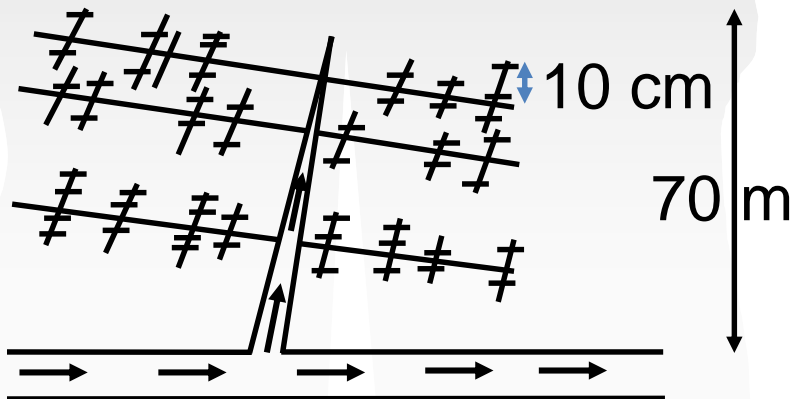
$1/p = c_g$ = gas compressibility

c_ϕ = shale compressibility

ϕ = shale porosity

k = shale permeability

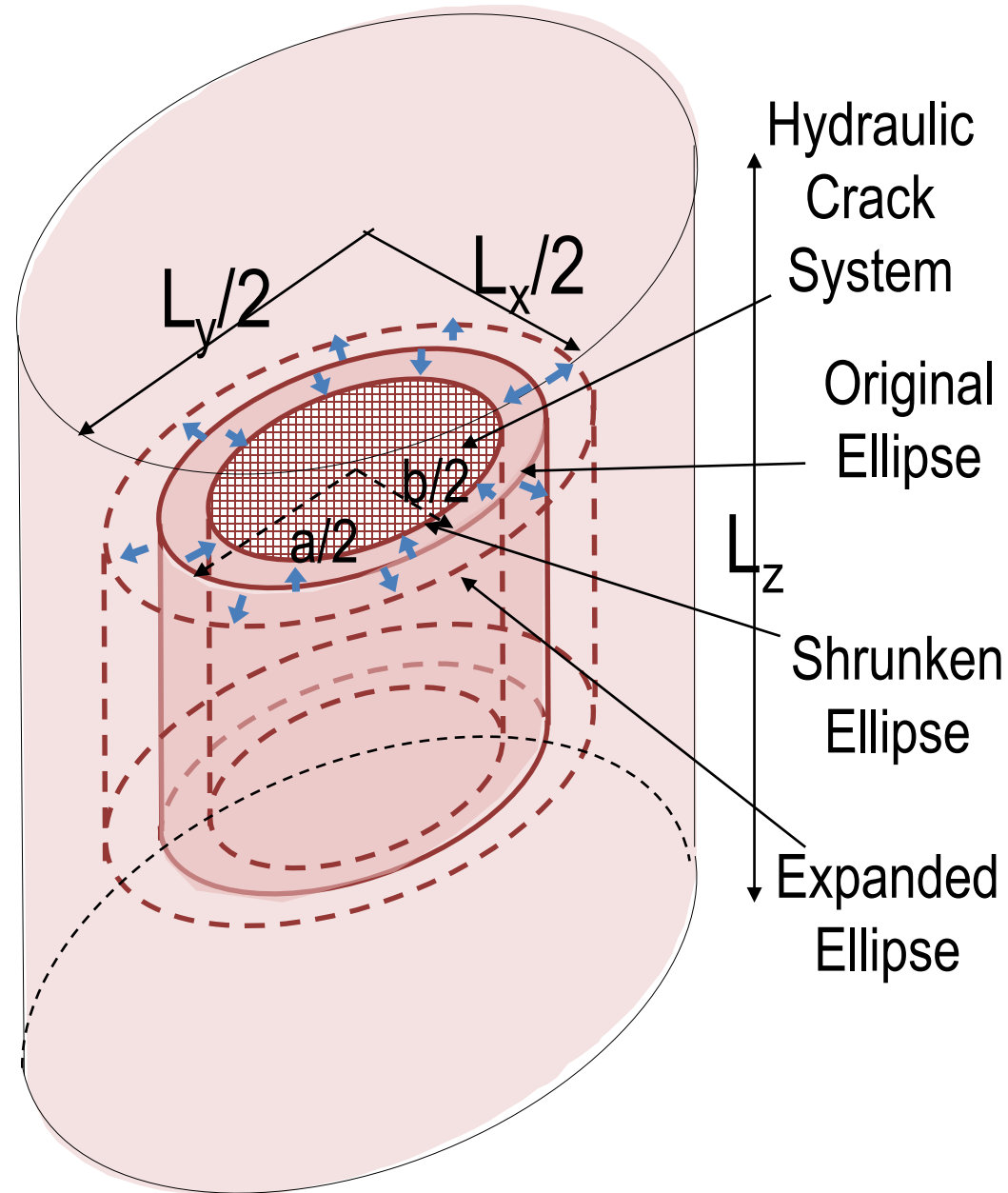
μ = gas viscosity



Volume of all cracks

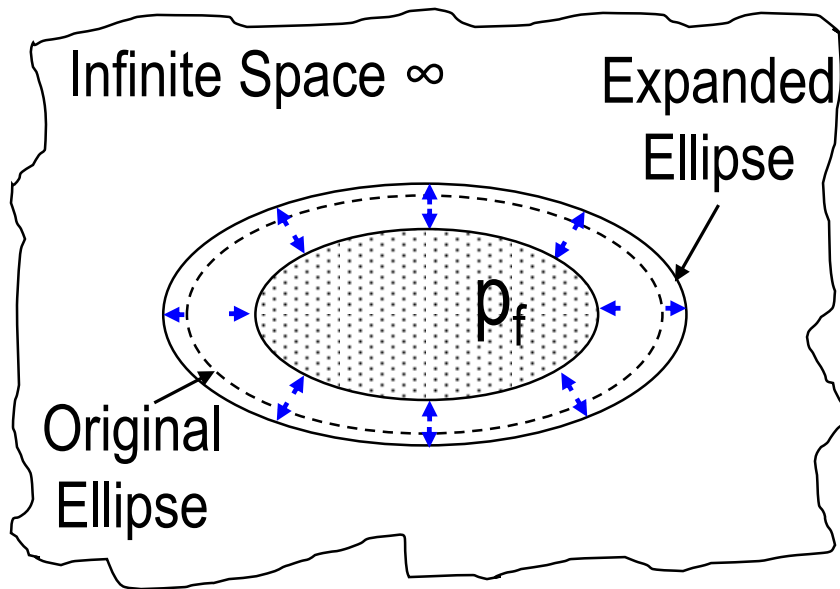
= expansion of
fracking zone (approx.
an elliptical cylinder)
in infinite space

+ elastic contraction
of shale between
cracks



Calculation of Volume of All Hydr. Cracks in Fracking Stage

To find an analytical formula, consider the fracking stage to be an elliptical cylinder in plane strain, in infinite space



Elliptical coordinates:

$$z = c \cosh \zeta \quad \zeta = \xi + i\eta$$

Complex potentials (Stevenson 1945):

$$\psi(z) = \frac{p_f c}{2} (\sinh \zeta - \cosh \zeta)$$

$$\chi(z) = -\frac{p_f c^2}{2} \zeta \cosh 2\xi_0$$

Displacement field:

$$u_x + iu_y = 1/2G[(3 - \nu)/(1 + \nu)\psi(z) - z\bar{\psi}(\bar{z}) - \bar{\chi}'(\bar{z})]$$

(e.g., Timoshenko -Goodier1970)

Calculation of Volume Expansion of Elliptic Cylinder

$$u_x = \frac{p_f c \sinh \xi \cos \eta}{2G(1 + \nu)} \frac{\Pi(\xi, \eta) - (1 - \nu) \coth \xi}{\cosh 2\xi - \cos 2\eta}$$

$$u_y = \frac{p_f c \cosh \xi \sin \eta}{2G(1 + \nu)} \frac{\Pi(\xi, \eta) - (1 - \nu) \tanh \xi}{\cosh 2\xi - \cos 2\eta}$$

$$\Pi(\xi, \eta) = (1 - \nu) \cosh 2\xi + (1 + \nu) \cosh 2\xi_0 - 2 \cos 2\eta$$

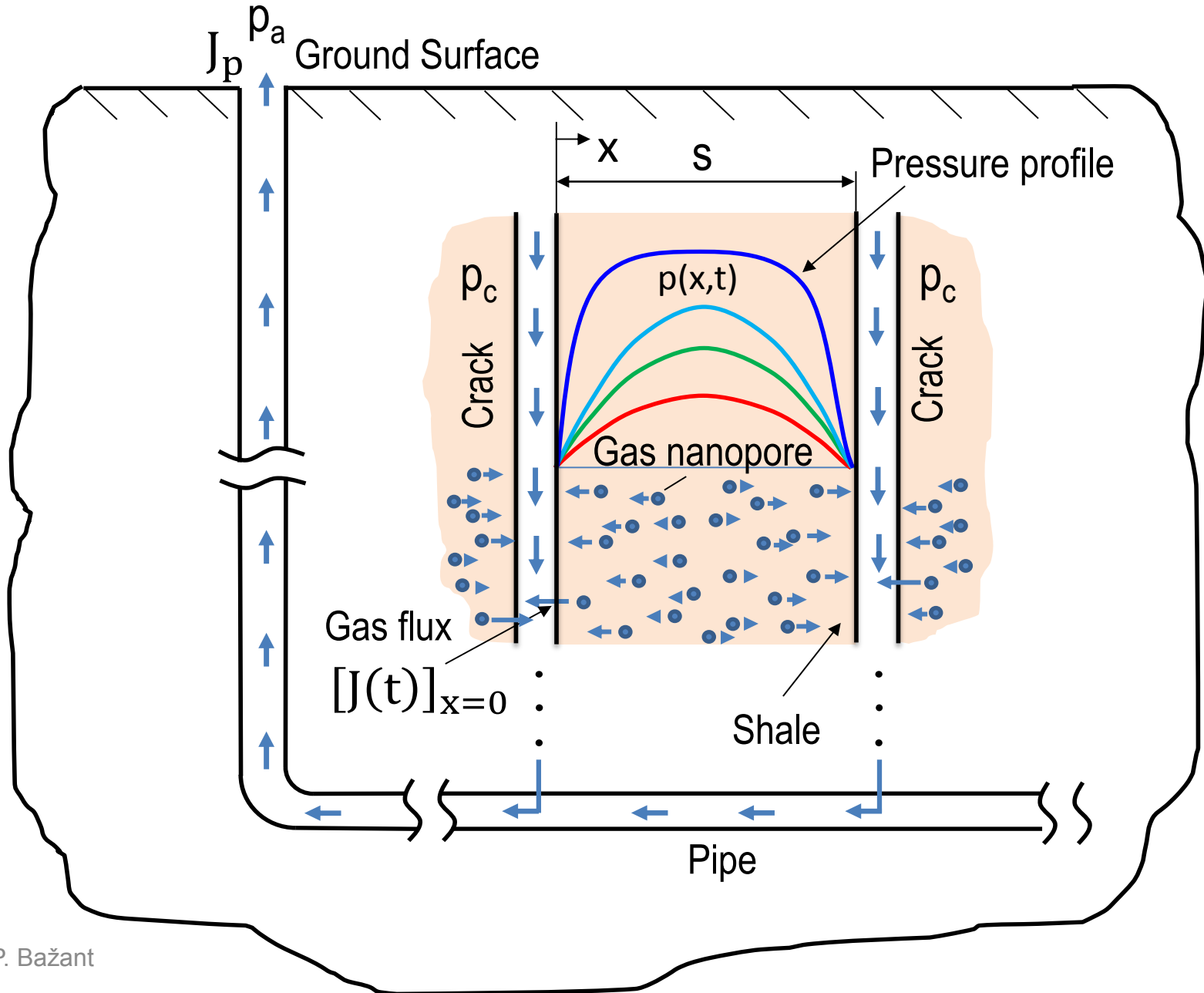
Curvilinear displacement components: $u_\xi + iu_\eta = e^{-i\alpha}(u_x + iu_y)$

$$u_\xi = \frac{u_x \sinh \xi \cos \eta + u_y \cosh \xi \sin \eta}{\sqrt{1/2(\cosh 2\xi - \cos 2\eta)}}$$

Expansion (exploiting symmetry of the problem):

$$\Delta V = 4L_z \int_0^{\pi/2} u_\xi(\eta) c \cosh \xi_0 d\eta$$

Transport of Gas from Shale to Surface



Gas Transport Model

Diffusion of Gas Through the Shale Toward the Hydraulic Cracks

Darcy's law:

$$v = -\frac{k}{\mu} \frac{\partial p}{\partial x}$$

Mass conservation:

$$\frac{\partial(\phi\rho)}{\partial t} + \frac{\partial(\rho v)}{\partial x} = 0$$

Shale Porosity Gas Dynamic Viscosity

$$\frac{\phi\mu}{k} \left(C_s + \frac{1}{p} \right) \frac{\partial p}{\partial t} = \frac{1}{p} \frac{\partial}{\partial x} \left(p \frac{\partial p}{\partial x} \right)$$

Shale Compressibility

Transport of Gas from Crack System to Surface

Gas flux from shale surface

into cracks: $J = -\frac{k}{\mu} \left[\frac{\partial p}{\partial x} \right]_{x=0}$

Hagen–Poiseuille law for gas

flow in pipe: $J_p = -\frac{b_1}{\mu L} \left(\frac{p_c^2 - p_a^2}{p_a} \right)$

Mass balance condition:

$$\frac{dm_c}{dt} = J_p - A_c J = \rho V_c C_g \frac{dp_c}{dt}$$

Gas Compressibility

shale permeability

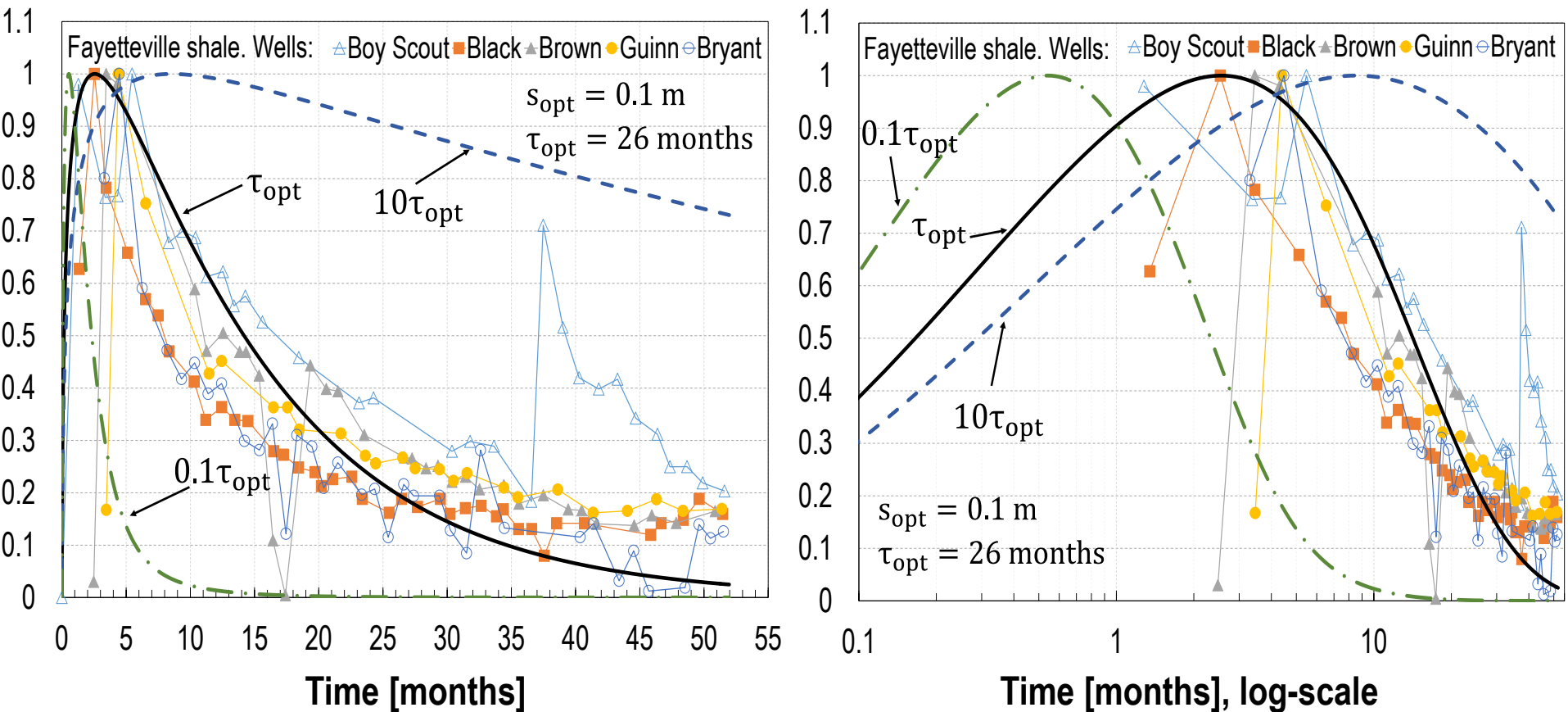
$$\frac{dp_c}{dt} + \frac{p_c}{\tau} \frac{p_c^2 - p_a^2}{p_a^2} = \frac{A_1 k}{\mu} p_c \left[\frac{\partial p}{\partial x} \right]_{x=0}$$

$$\tau = LV_c \mu / b_1 p_a = \text{characteristic time}$$

$$A_1 = A_c / V_c \quad \text{Total Crack Volume}$$

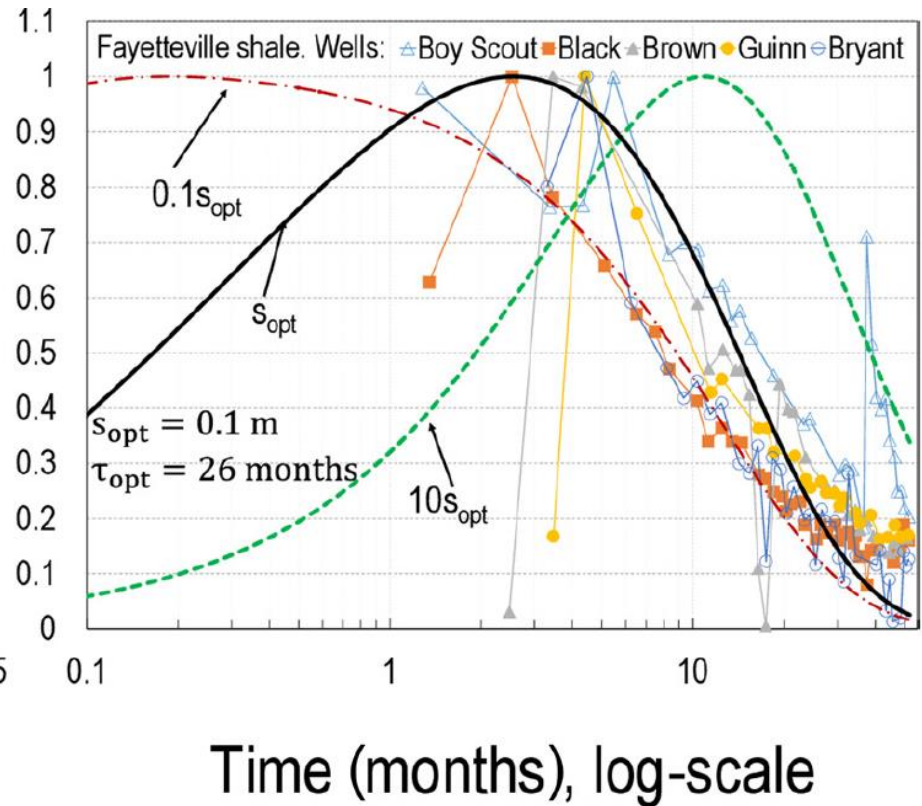
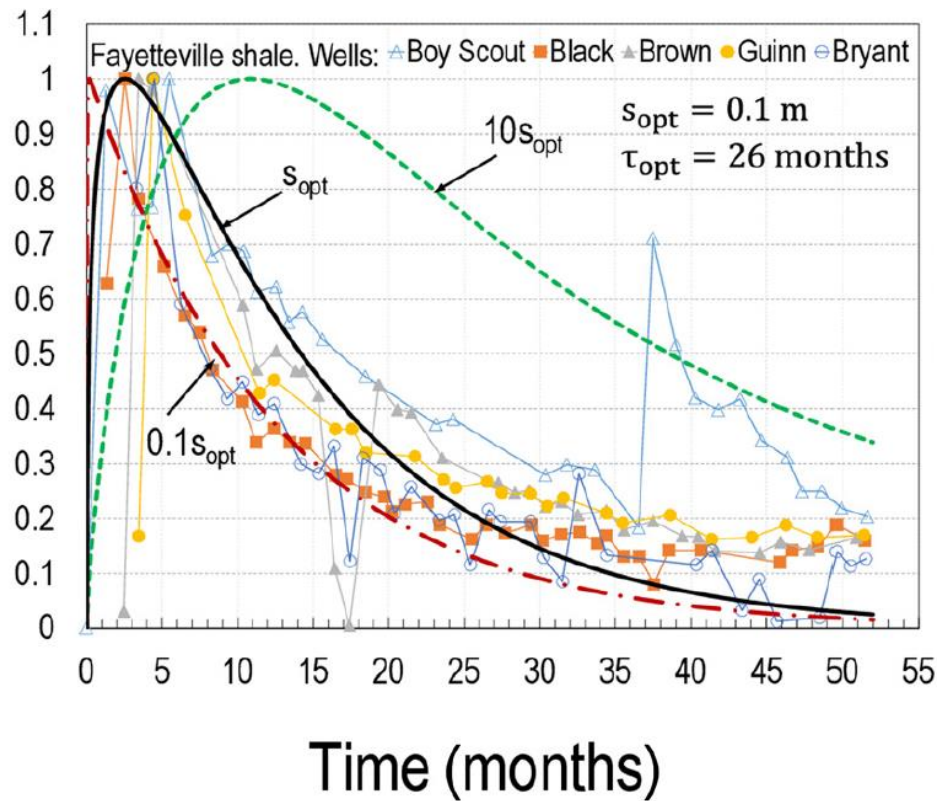
Surface Area of Cracks

Effect of 10-fold change of characteristic time, τ_{opt}

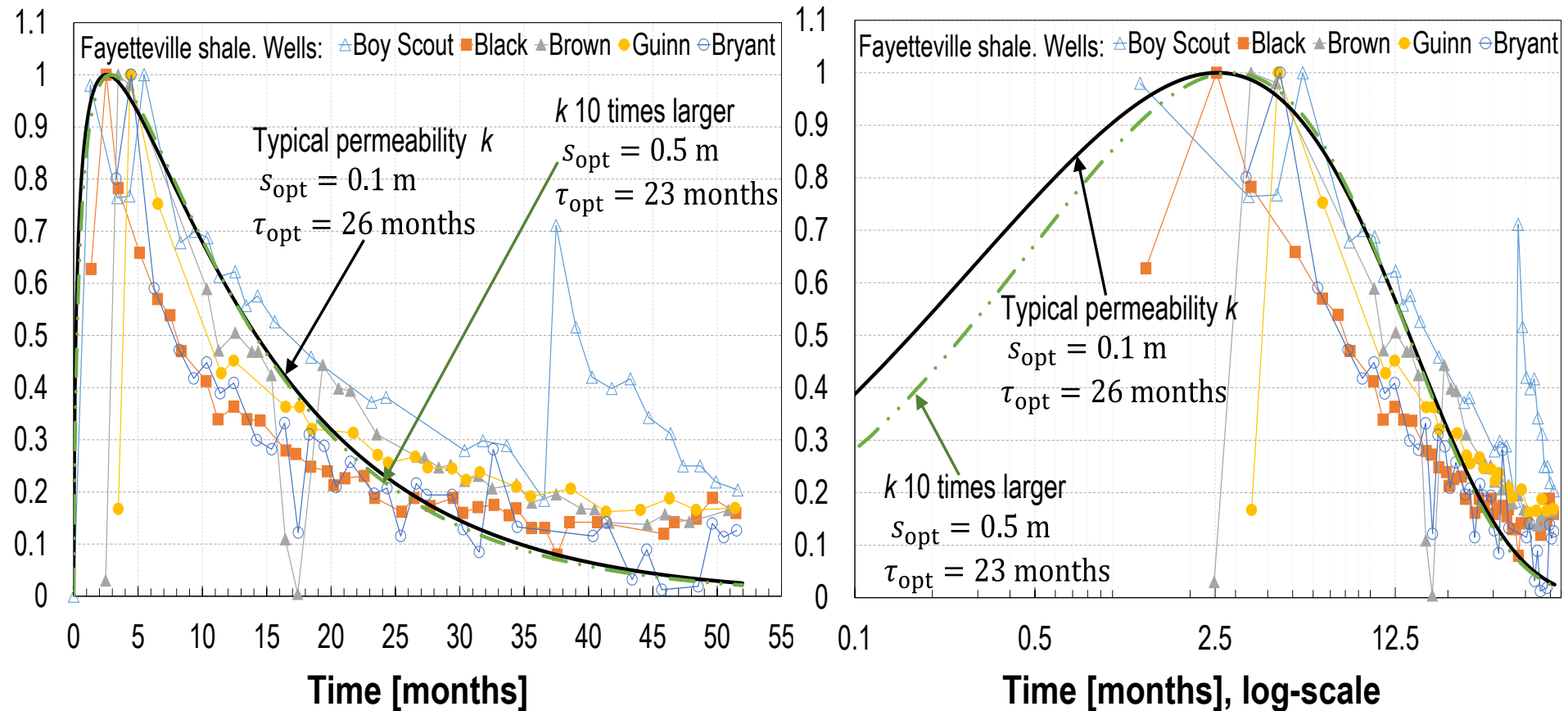


Time histories of gas flux observed on the surface

Effect of 10-fold change crack spacing, s



Effect of 10-fold change of permeability, k



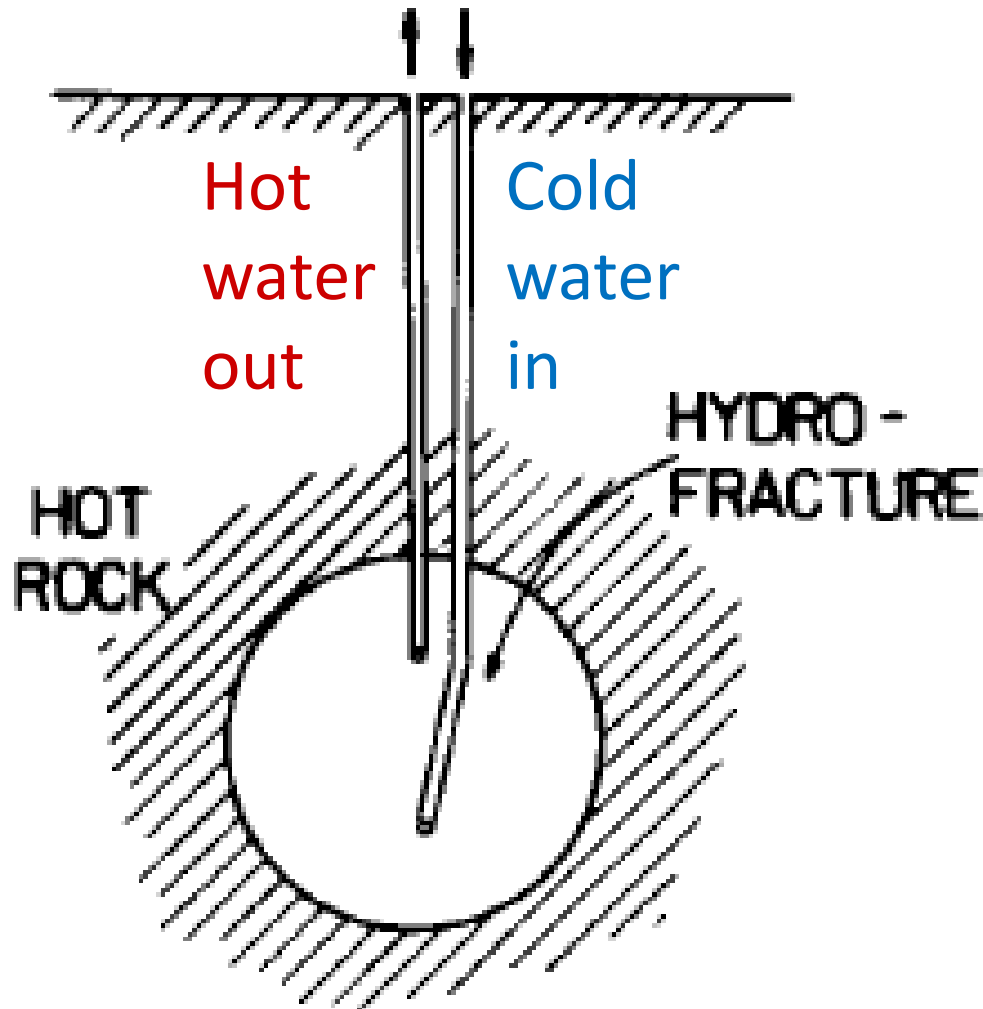
— *much weaker than the effects of crack spacing and of characteristic time*

Conclusion from Diffusion Analysis

- If the gas flux peak occurs in about 2.5 months and 50% flux reduction in about 16 months, the spacing of hydraulic cracks and open joints in Fayetteville shale must be about 10 cm.
- For 1 m spacing (a 10-fold increase), the 50% flux reduction occurs in about 125 years.
- For a 3 m spacing, about 12,000 years.
- For a 10 m spacing, about 125,000 years.
- For a 1 cm spacing, about 4 days.

*How to Achieve Small
Enough Crack Spacing
over a Large Zone?*

Concept of the Unsuccessful 1970s Hot Dry Rock Geothermal Energy Scheme¹

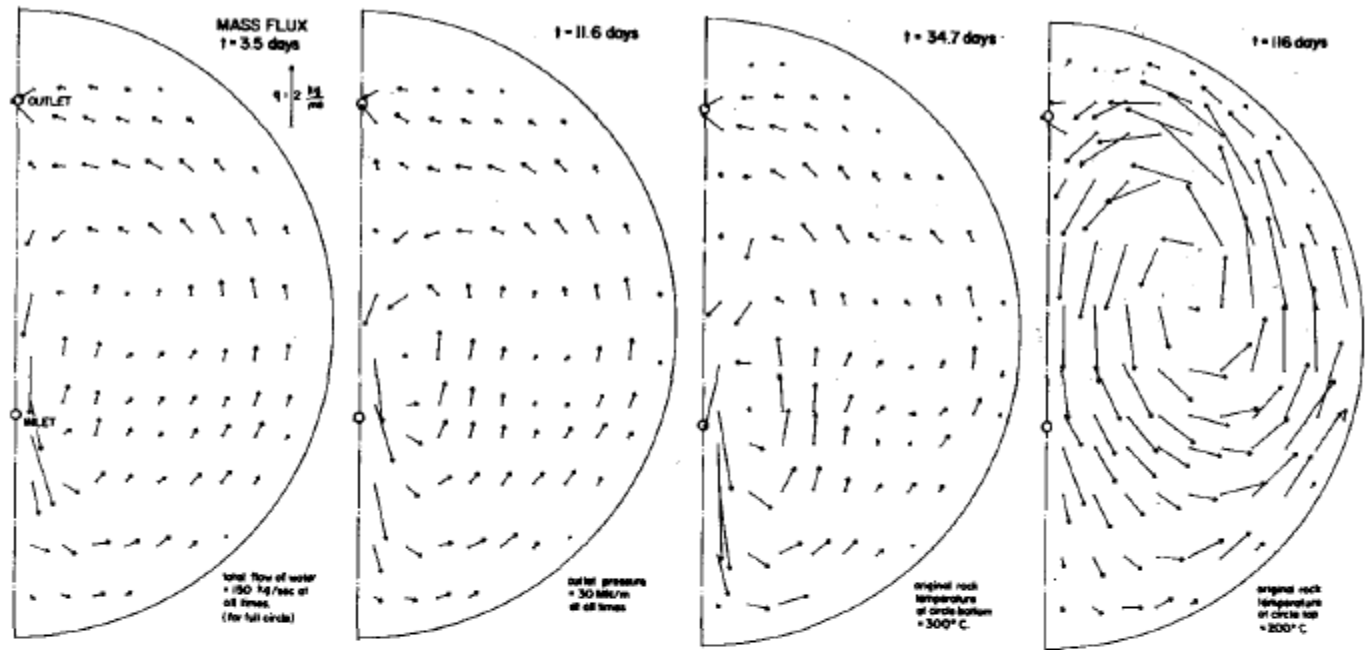


LASL drilled a well in Valles Caldera, Jemez Mountains and created a large fracture

¹NU-LASL Collaborative Project 1974-77.

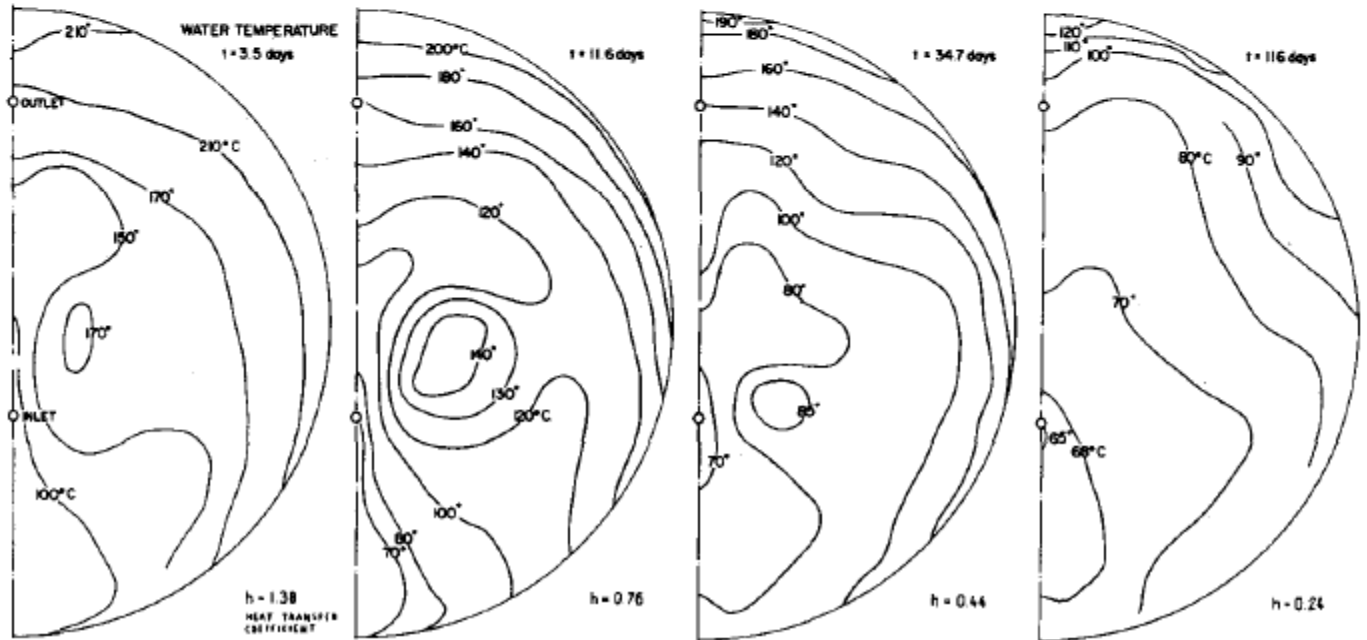
NU investigators:
J Weertman, PI
JD Achenbach
ZP Bazant
J Dundurs
LM Keer
T Mura
S Nemat-Nasser

1970s NU-LASL Hot Dry Rock Geothermal Energy Project



**Hydro-crack
diameter 1 km.
Granite,
T = 300°C.**

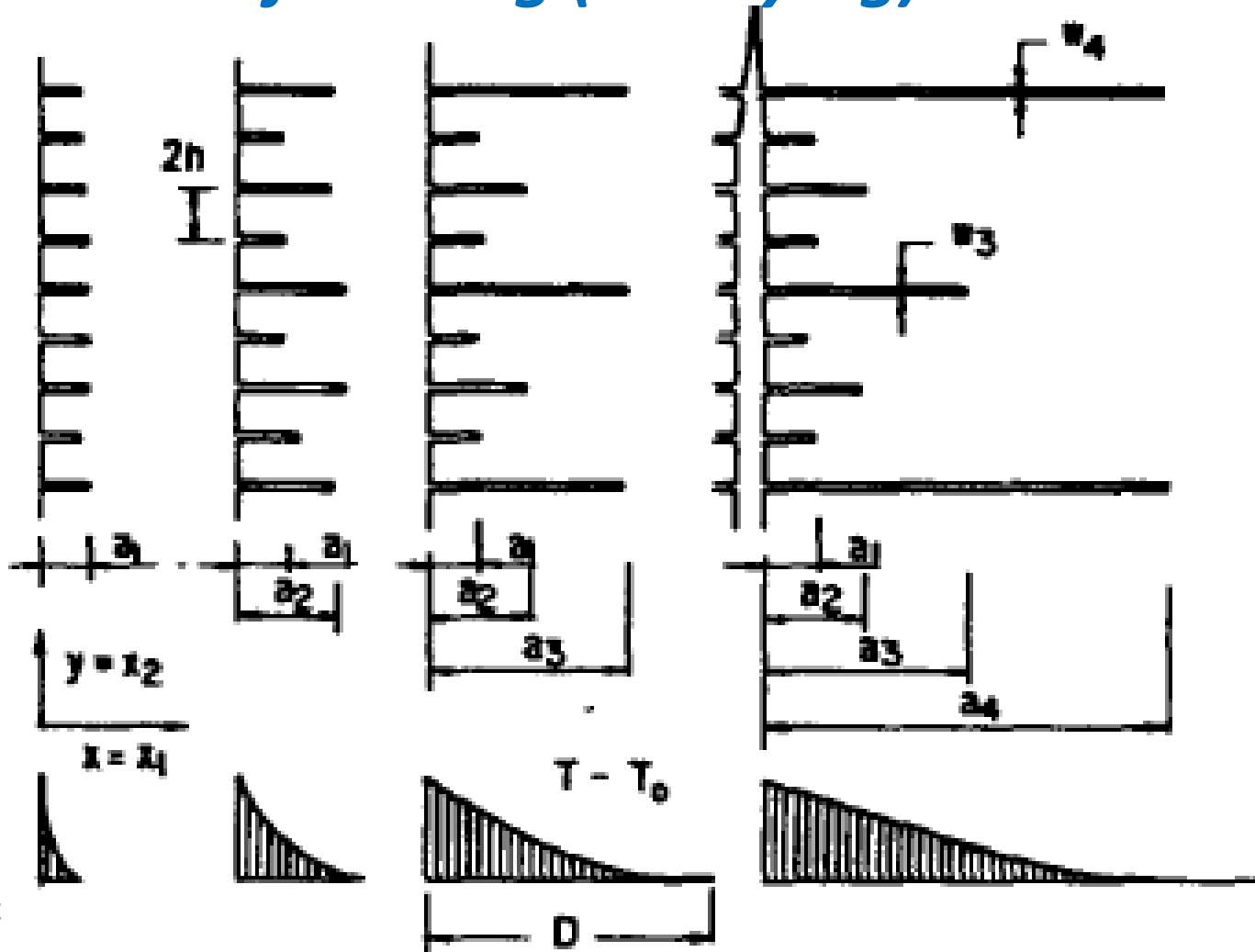
**Water out:
initially
T₁ = 210°C.
After 116 days:
90°C.**



Localization Instability of Crack System

NU-LASL Hot Dry Rock Geothermal Energy Project, 1976

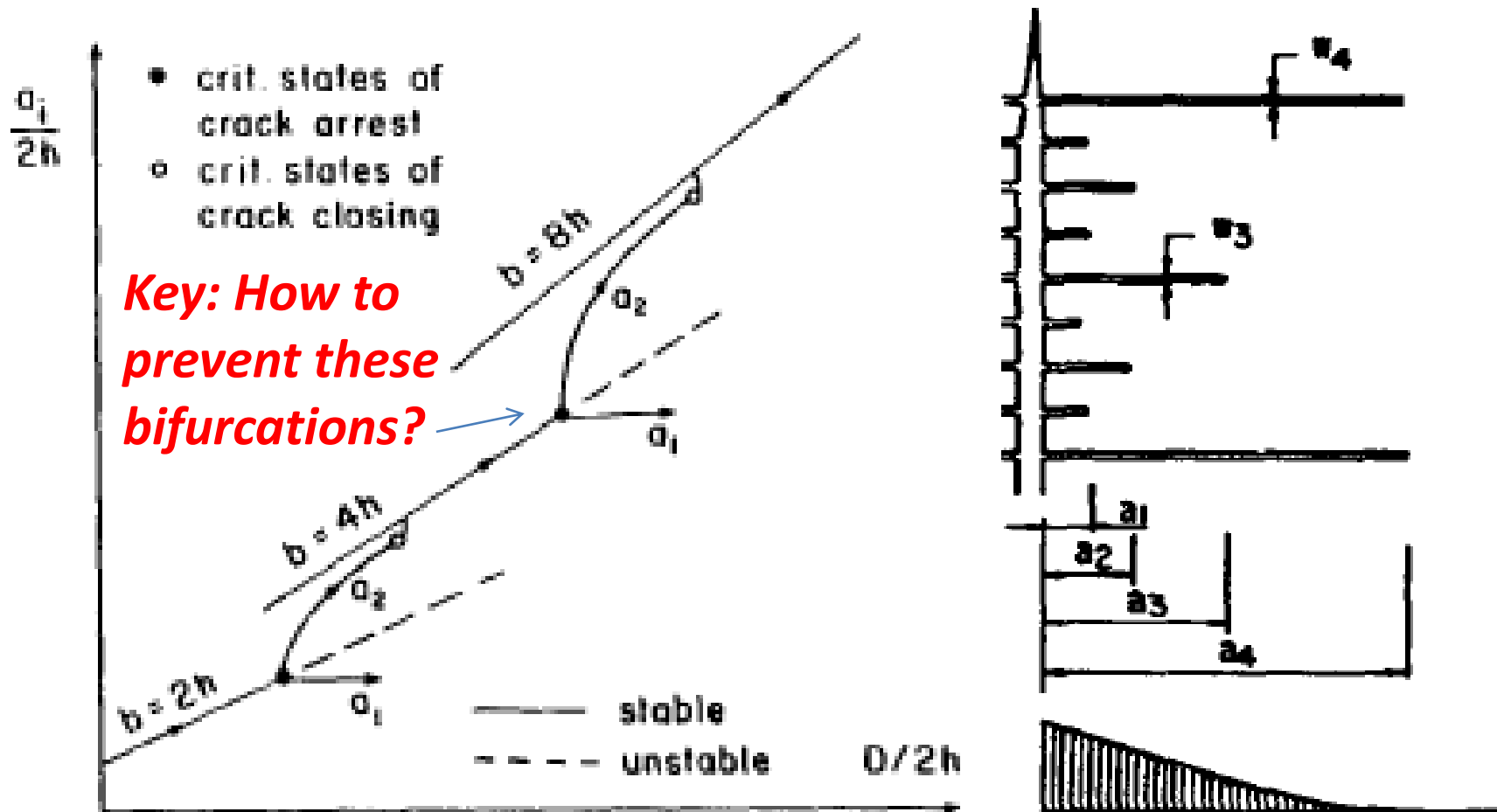
Evolution of Cooling (or Drying) Cracks



ZP Bazant,
H Ohtsubo,
Mech.
Res. Comm.
4 (5), 353-
366 (1977);
and
Int. J. of
Fracture 15,
443—456
(1979)

Max. Crack Depth vs. Penetration Front Depth in Localizing Parallel Crack System

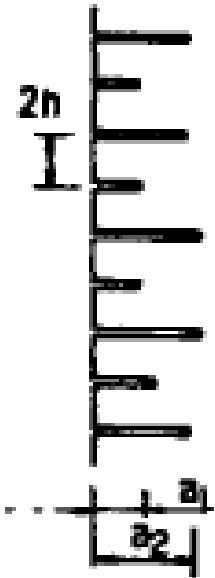
1976 NU-LASL Geothermal Energy Project



Stability of Crack System

Helmholtz Free Energy of Crack System:

Array of parallel cracks



$$F = U(a_1, a_2, \dots, a_N; p) + \sum_{i=1}^N \int \Gamma da_i$$

a_i = i -th crack length Γ = fracture energy
 p = loading parameter: crack pressure or ΔT

U = strain energy of the elastic body

Taylor's series expansion: $\Delta F = \delta F + \delta^2 F + \dots$

For m growing cracks and $n-m$ shortening ones:

$$\delta F = \sum_{i=1}^m \left(\frac{\partial U}{\partial a_i} + \Gamma \right) \delta a_i + \sum_{j=m+1}^n \left(\frac{\partial U}{\partial a_j} \right) \delta a_j$$

$$\delta^2 F = \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n \left(\frac{\partial^2 U}{\partial a_i \partial a_j} \right) \delta a_i \delta a_j = \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n F_{ij} \delta a_i \delta a_j$$

$$\delta a_i > 0 \quad i = 1, \dots, m$$

$$\delta a_i < 0 \quad i = m + 1, \dots, n$$

$$\delta a_i = 0 \quad i = n + 1, \dots, N$$

Equilibrium condition: $\delta F > 0$

$$\text{for } \delta a_i > 0 : -\frac{\partial U}{\partial a_i} = \Gamma \quad \text{or } K_i = K_{Ic}$$

$$\text{for } \delta a_i < 0 : -\frac{\partial U}{\partial a_i} = 0 \quad \text{or } K_i = 0$$

Stability conditions: $\Delta F > 0$ for all δa_i ... **positive definite**

If $\delta F = 0$, stability will be ensured if:

$$2\delta^2 F = \sum_{i=1}^n \sum_{j=1}^n F_{,ij} \delta a_i \delta a_j > 0 \text{ for any admissible } \delta a_i$$

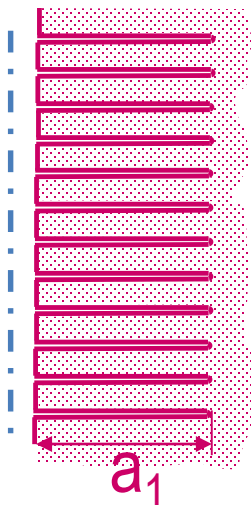
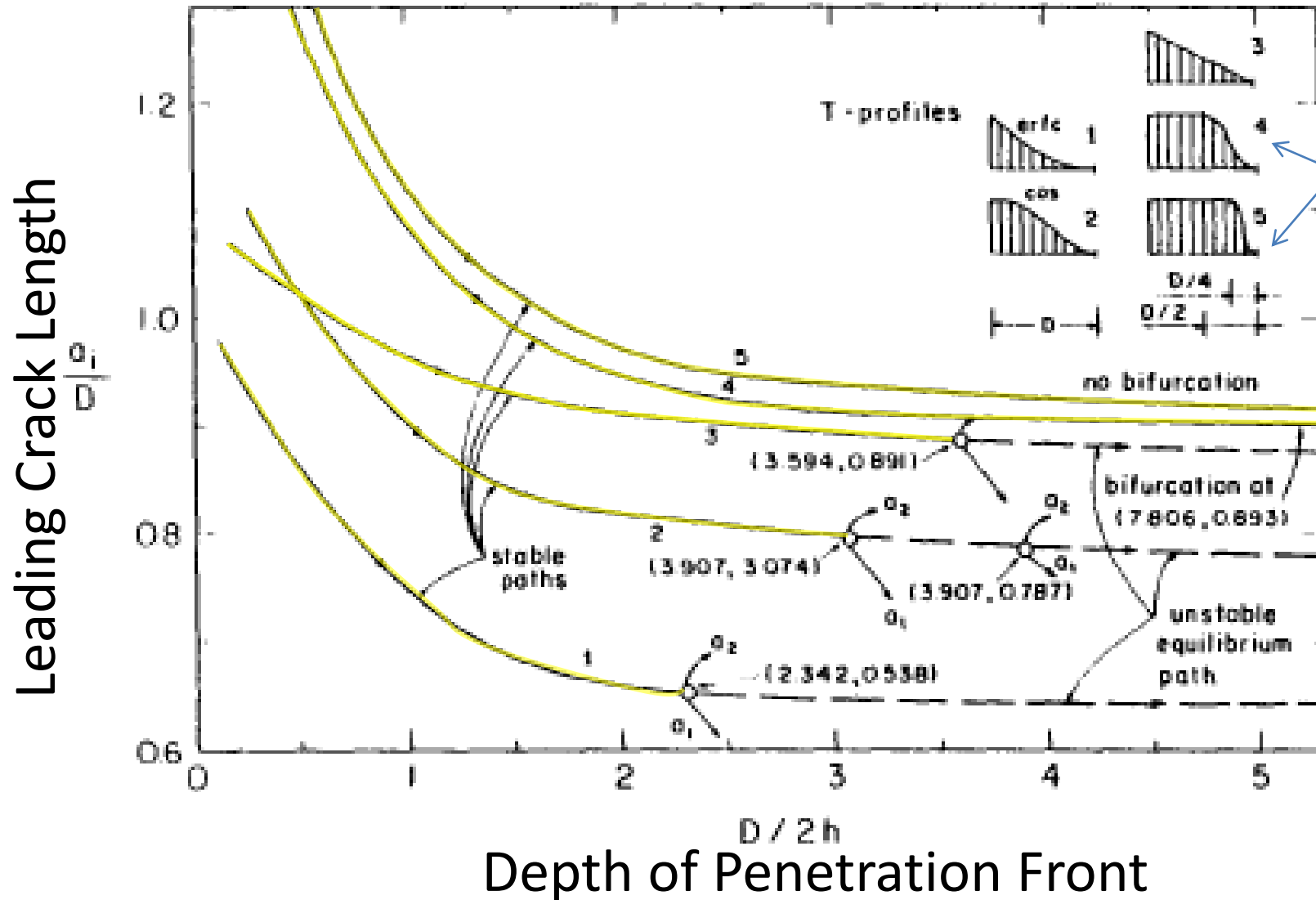
For 2 alternating crack lengths:

$$F_{,11} = F_{,22} > 0 \text{ and } \begin{vmatrix} F_{,11} & F_{,12} \\ F_{,21} & F_{,22} \end{vmatrix} > 0$$

Front Steepness: Key to Prevent Localization

1976 NU-LASL Geothermal Energy Project

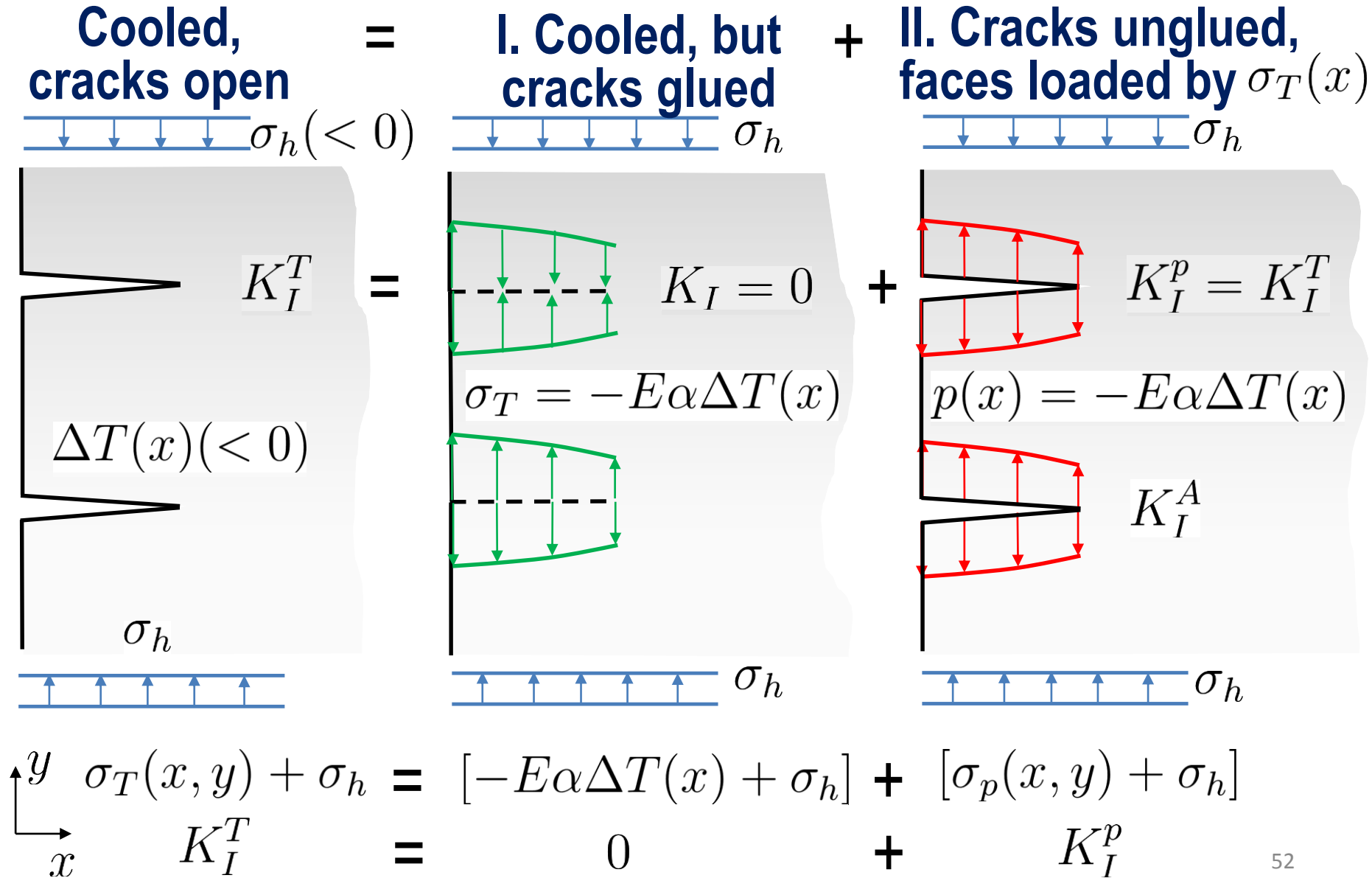
For a steep front, cracks don't localize!



Lesson from the 1970s project

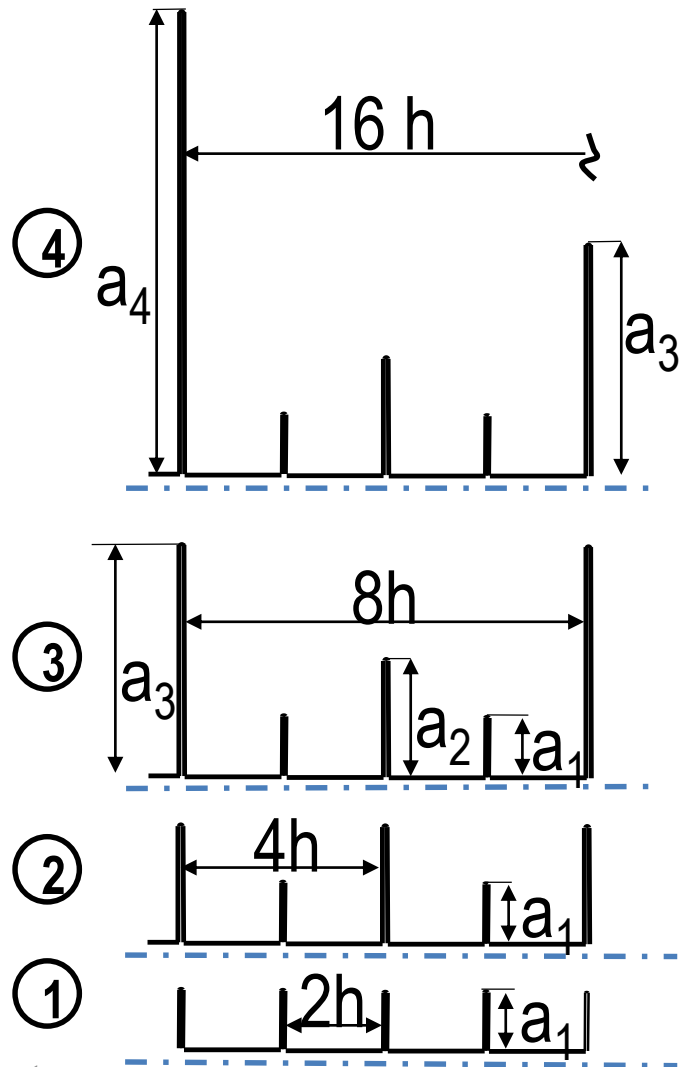
- Stability of crack system is an essential part of hydraulic fracturing analysis (ignored so far)
- Localization can be prevented and a parallel crack system can be produced if and only if the **pressure profile is nearly uniform over a long enough portion of the crack.**

Hydro-Thermal Analogy for Periodic LEFM Cracks

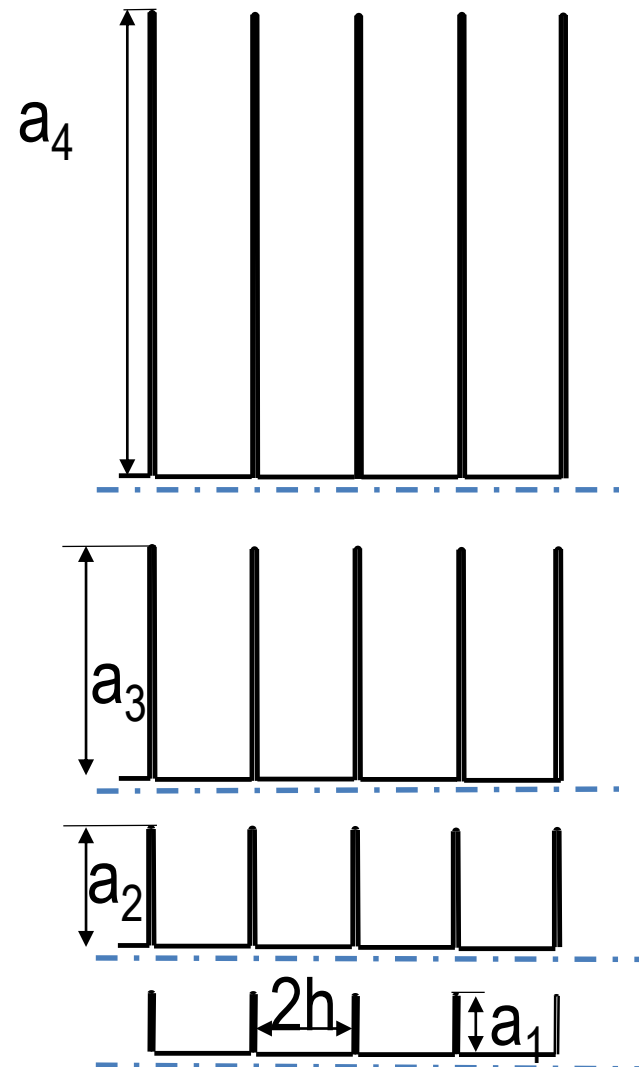


Circular Crack Localization

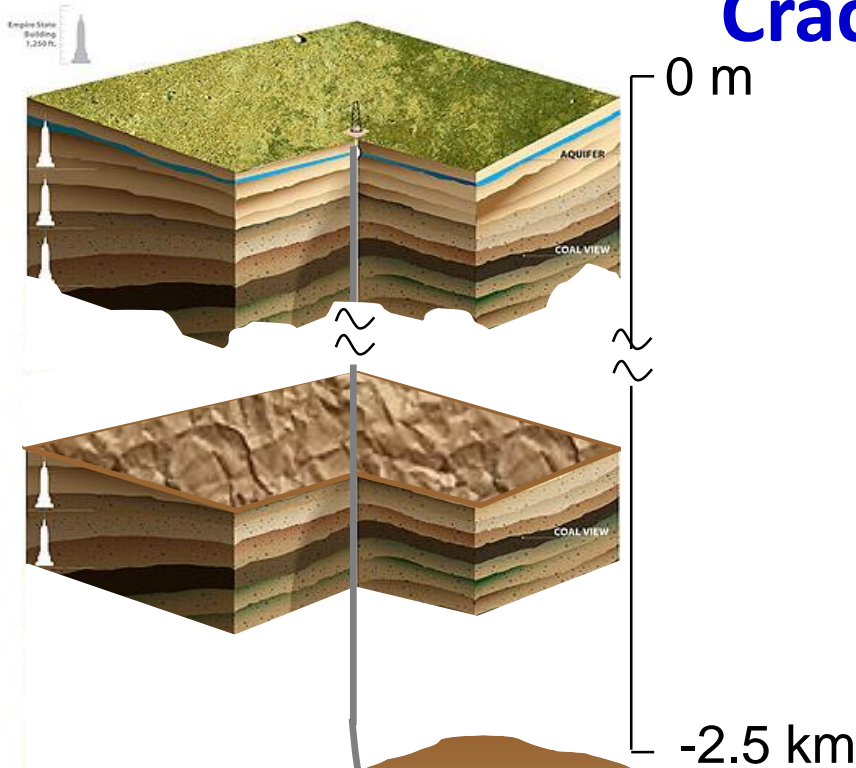
a) To avoid



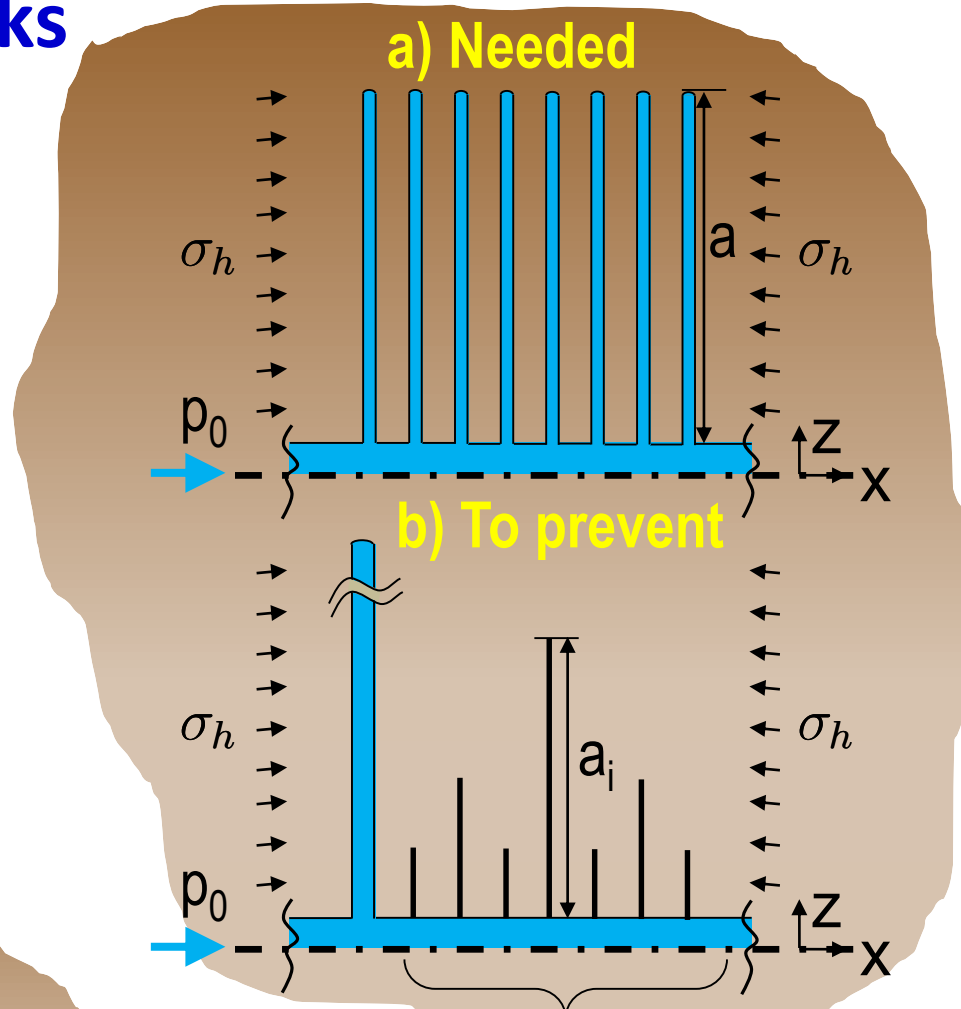
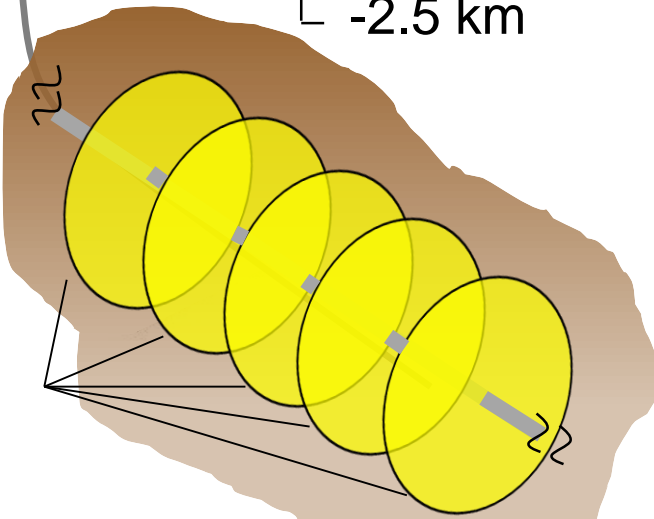
b) Needed



Localization Instability of Fluid-Pressurized Circular Cracks



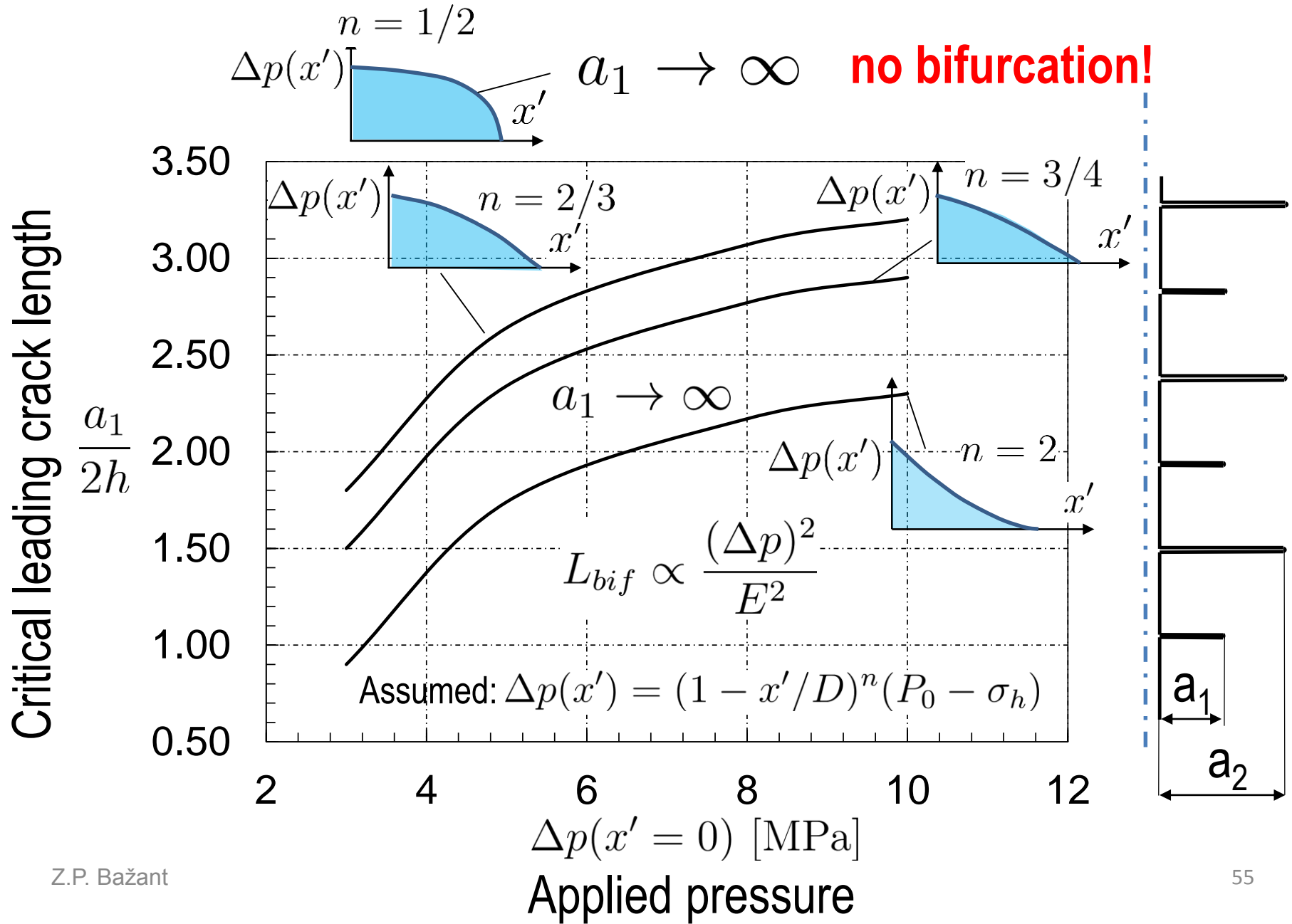
Cracks, initially quasi-circular (later quasi-rectangular)



Cracks that have closed

p_0 = borehole pressure
 σ_h = minimum horiz. stress

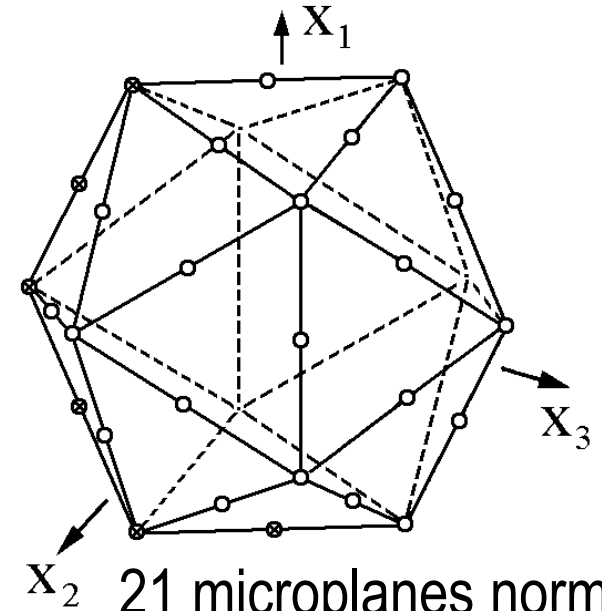
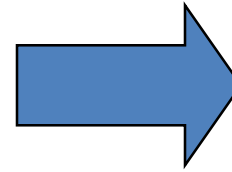
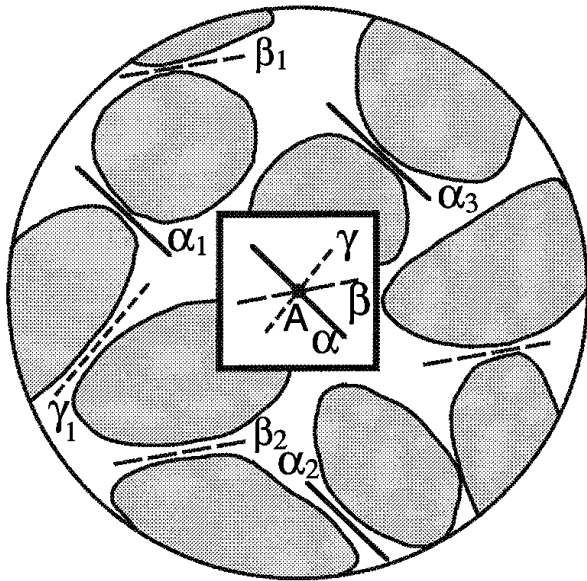
Effect of Front Steepness of Pressure Profile



Summary of Four Omitted Slides on Ongoing Research in Bažant's Group

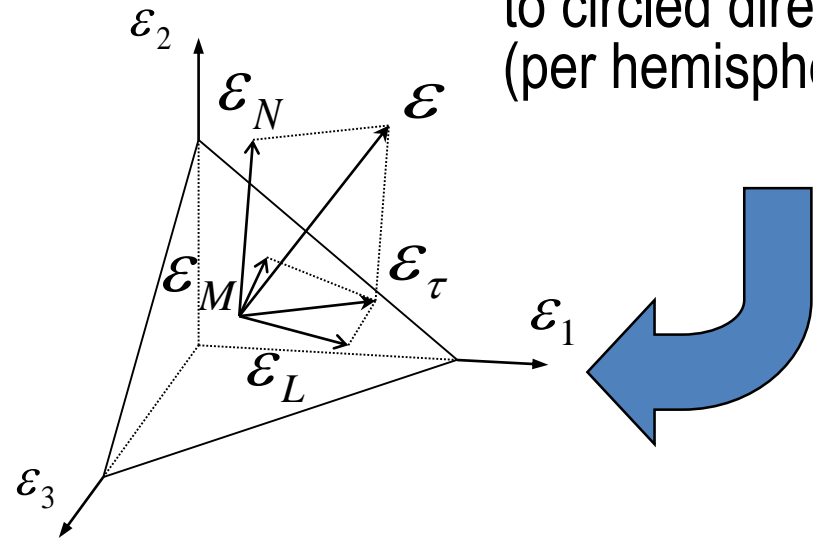
- Crack band model is used for a smeared continuum model of evolution of a fracking stage with millions of existing or potential cohesive cracks.
- The continuum model is discretized by finite elements.
- Viscous pressurized compressible fluid flows through a 3D system of cracks in shale.
- Cracks interact with each other through the rock with each other.
- Crack localization affects the flow of fluid.

Microplane — a Semi-Multiscale Model



21 microplanes normal to circled directions (per hemisphere)

Subscale interactions among orientation are captured (lumped into a continuum point) but interactions at distance are not



Microplane strain components

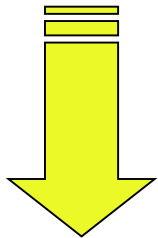
General Algorithm in Microplane Model

Kinematic constraint

Macro-Strain
 ϵ_{ij}



Micro-Strains
 $\epsilon_N, \epsilon_V, \epsilon_D, \epsilon_L, \epsilon_M$
on each plane



Classical
tensorial
models

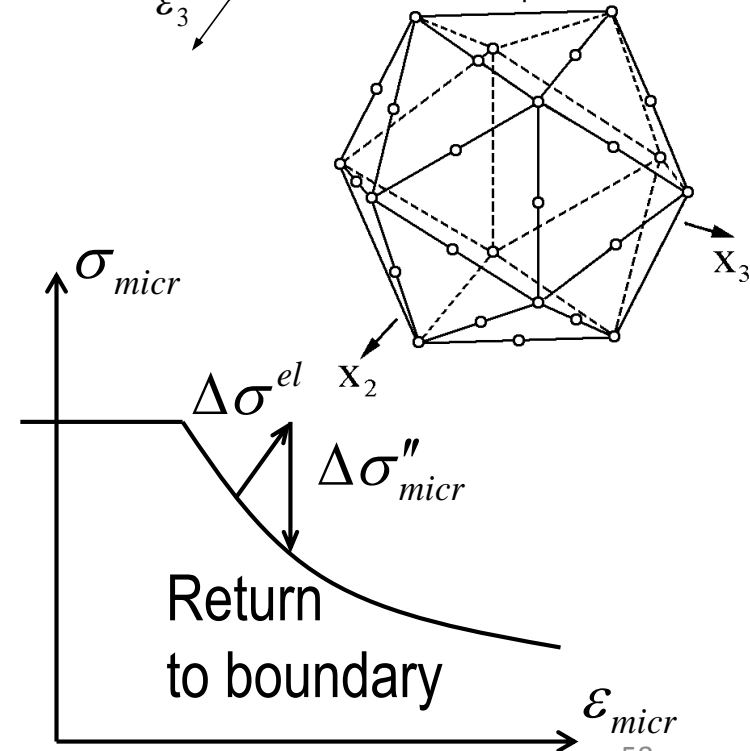
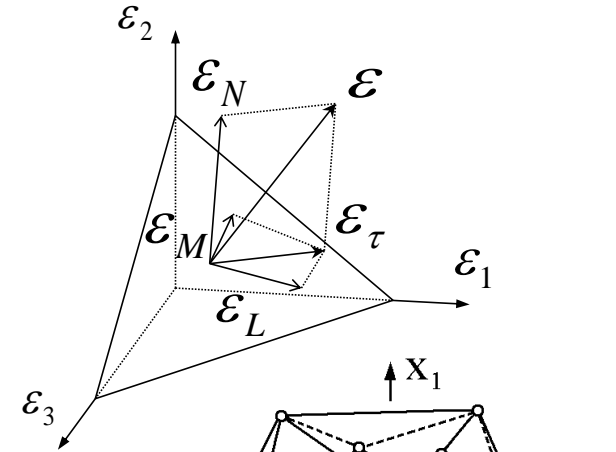
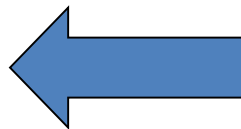
Macro-Stress
 σ_{ij}

**Microplane
constitutive
relation**



Micro-Stresses
 $\sigma_N, \sigma_V, \sigma_D, \sigma_L, \sigma_M$
on each plane

Principle of virtual work



Microplane Model for Anisotropic Shale*

$$\Delta\sigma_e = K_e\Delta\epsilon$$

K_e = transversely isotropic elasticity tensor

$$\Delta\sigma_N^e = n^T \cdot \Delta\sigma_e \cdot n; \quad \Delta\sigma_\tau^e = n^T \cdot \Delta\sigma_e - \Delta\sigma_N^e n$$

$$\sigma_N = \max\left(\sigma_V^b + \sigma_D^b; \min(\sigma_N^b; \sigma_N^0 + \Delta\sigma_N^e)\right)$$

$$\sigma_\tau = \min(\sigma_\tau^b; \sigma_\tau^0 + \Delta\sigma_\tau^e); \quad \sigma_L = \sigma_\tau \cos(\alpha); \quad \sigma_M = \sigma_\tau \sin(\alpha)$$

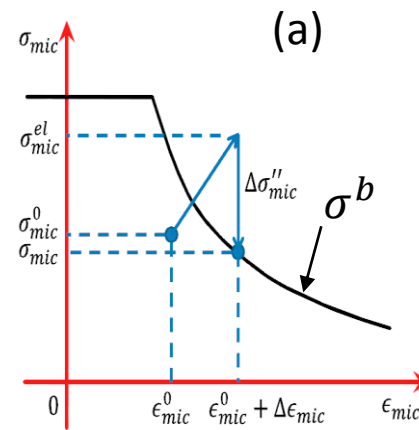
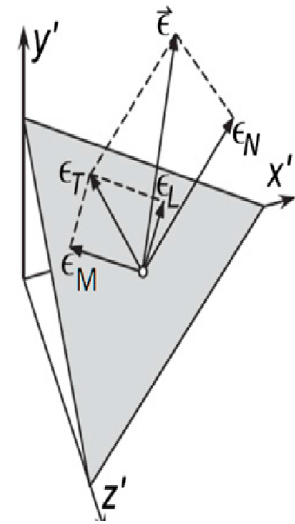
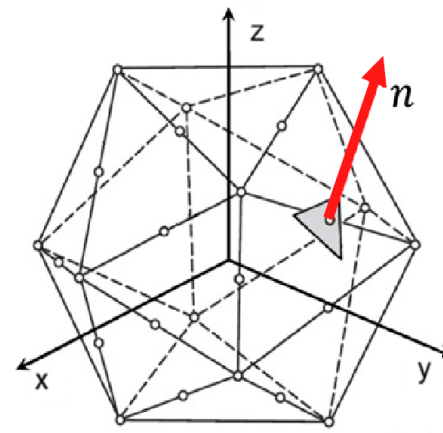
$$\sigma_V^b = \sqrt{\left(\frac{n_x}{\sigma_{Vx}^b}\right)^2 + \left(\frac{n_y}{\sigma_{Vt}^b}\right)^2 + \left(\frac{n_z}{\sigma_{Vt}^b}\right)^2}$$

$$\sigma_D^b = \sqrt{\left(\frac{n_x}{\sigma_{Dx}^b}\right)^2 + \left(\frac{n_y}{\sigma_{Dt}^b}\right)^2 + \left(\frac{n_z}{\sigma_{Dt}^b}\right)^2}$$

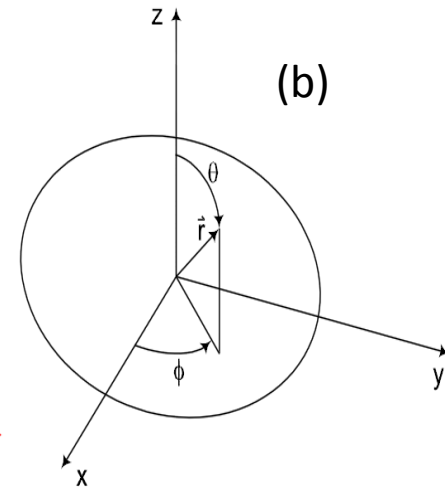
$$\sigma_N^b = \sqrt{\left(\frac{n_x}{\sigma_{Nx}^b}\right)^2 + \left(\frac{n_y}{\sigma_{Nt}^b}\right)^2 + \left(\frac{n_z}{\sigma_{Nt}^b}\right)^2}$$

x = direction normal to the bedding plane

y, z, t = directions in the bedding plane



(a)



(b)

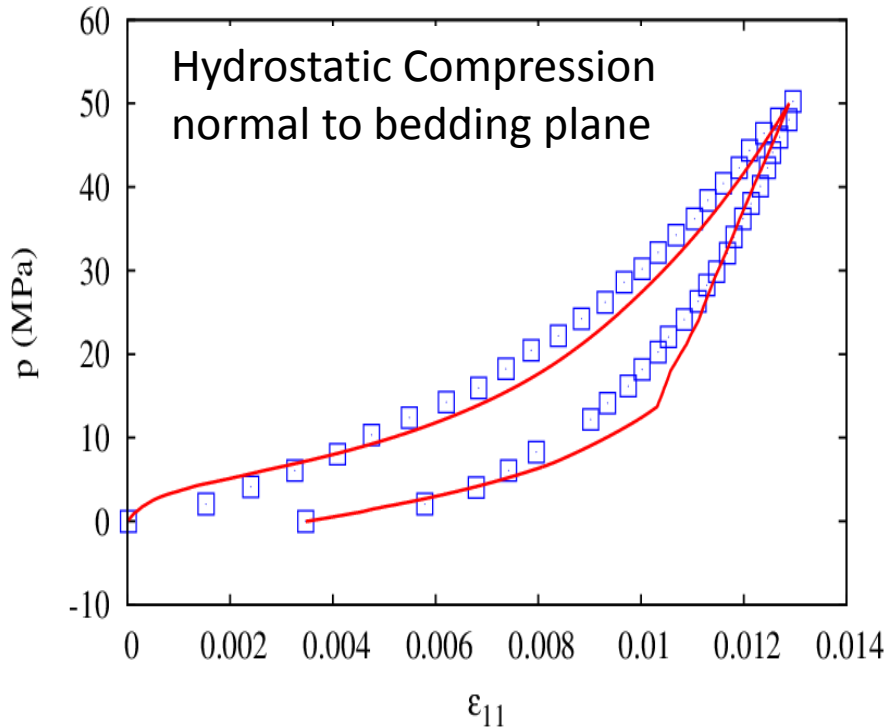
(c)

(d)

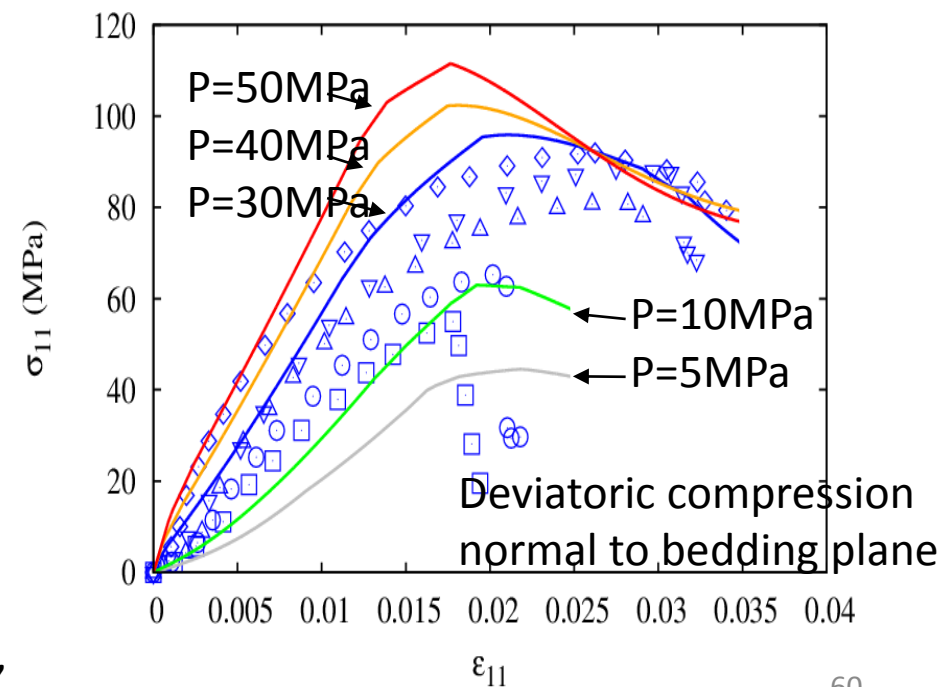
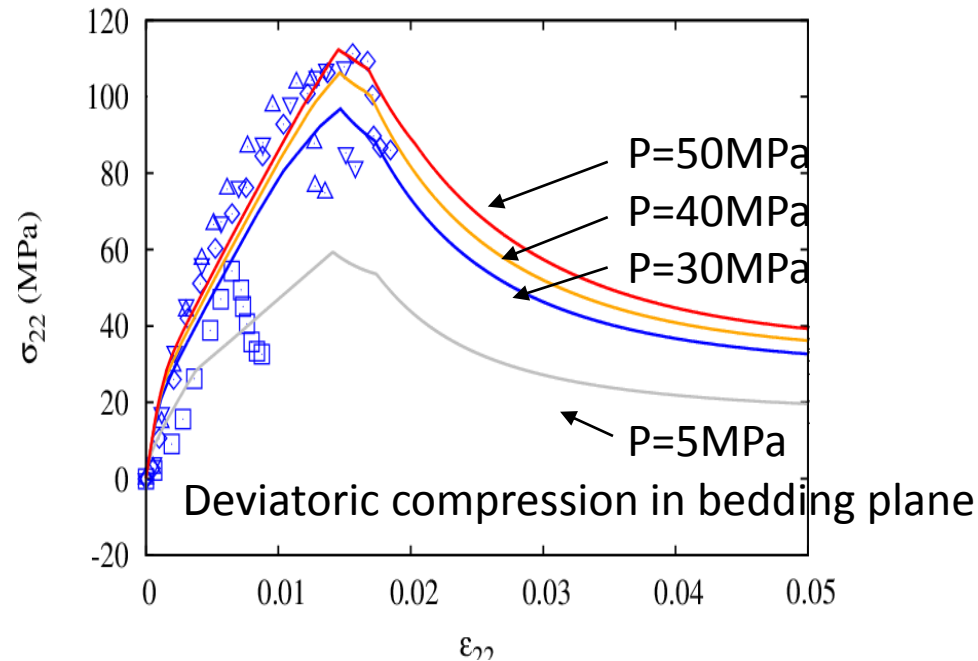
*By FC Caner,
& ZP Bazant

$$\sigma_{ij} = \int_{\Omega} \left(\sigma_N n_i n_j + \sigma_M \frac{1}{2} (n_i m_j + n_j m_i) + \sigma_L \frac{1}{2} (n_i l_j + n_j l_i) \right) d\Omega$$

Calibration of Microplane Model by Test Data



Test data: Niandou H, Shao JF, Henry JP and Fourmaintraux D (1997), "Laboratory investigation of the mechanical behavior of **Tournemire Shale**", Int. J. Rock Mech. Min. Sci., 34(1):3-16.



SUMMARY: Why Fracking Works

- The known 15% extraction percentage of gas content of shale implies formation of nonlocalized crack system.
- **Preventing localization is crucial.** Two ways to achieve it:
 - 1) Steep front of water pressure profile along the cracks, which can be achieved by appropriate pumping rate and history, proppant, viscosity control, acids, etc.;
 - 2) Cracking localization instability requires some cracks to close — prevented if the closing is blocked by proppant.

Thanks for listening!

Questions?

Google “Bazant”, download freely:

- 1) Bažant, Z.P., Salviato, M., Chau, Viet T., Viswanathan, H. and Zubelewicz, A. (2014). "Why fracking works." *ASME J. of Applied Mechanics* 81 (Oct.), 101010-1---101010-10.

Related works:

- 2) Bažant, ZP, FC Caner (Dec. 2013), **PNAS** 110 (48), 19291-19294;
- 3) Bažant, ZP, FC Caner (Feb. 2014), **JMPS** 139 (12), 714-1735.